

REGRET ANALYSIS AND BOUNDING

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MINIMAX REGRET ANALYSIS

Motivating Example

➤ Traditional way

Maximize Average...select A

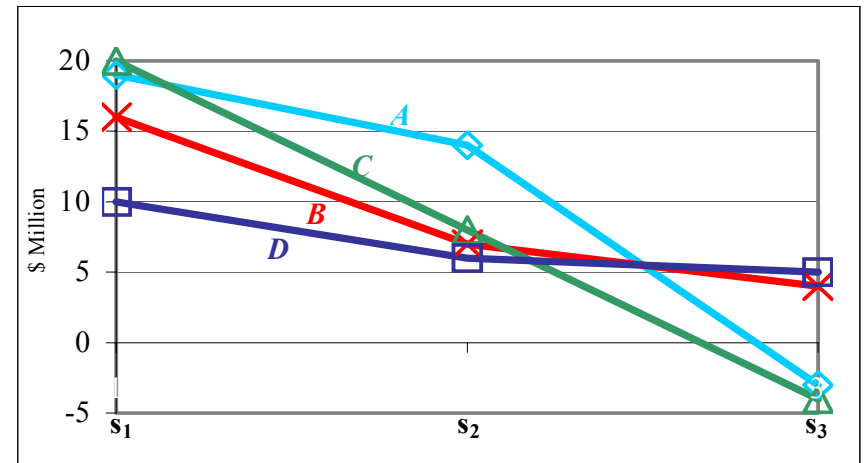
➤ Optimistic decision maker

MaxiMax ... select C

➤ Pessimistic decision maker

MaxiMmin ... select D

	S ₁ High	S ₂ Medium	S ₃ Low	Average
A	19	14	-3	10
B	16	7	4	9
C	20	8	-4	8
D	10	6	5	7
Max	20(C)	14(A)	5(D)	10(A)





MINIMAX REGRET ANALYSIS

Motivating Example

➤ Calculate regret:

find maximum regret

➤ A ... regret = 8 @ low market

➤ C ... regret = 9 @ low market

➤ D ... regret = 10 @ high market

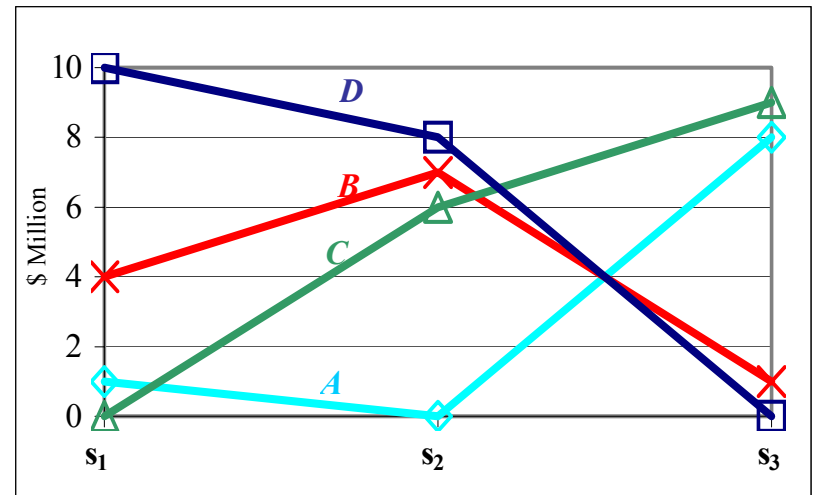
➤ B ... regret = 7 @ medium market

➤ **MINIMAX** → **B**

➤ In general, gives *conservative* decision

but not pessimistic.

	S ₁ High	S ₂ Medium	S ₃ Low	Maximum Regret
A	1	0	8	8
B	4	7	1	7
C	0	6	9	9
D	10	8	0	10





MINIMAX REGRET ANALYSIS

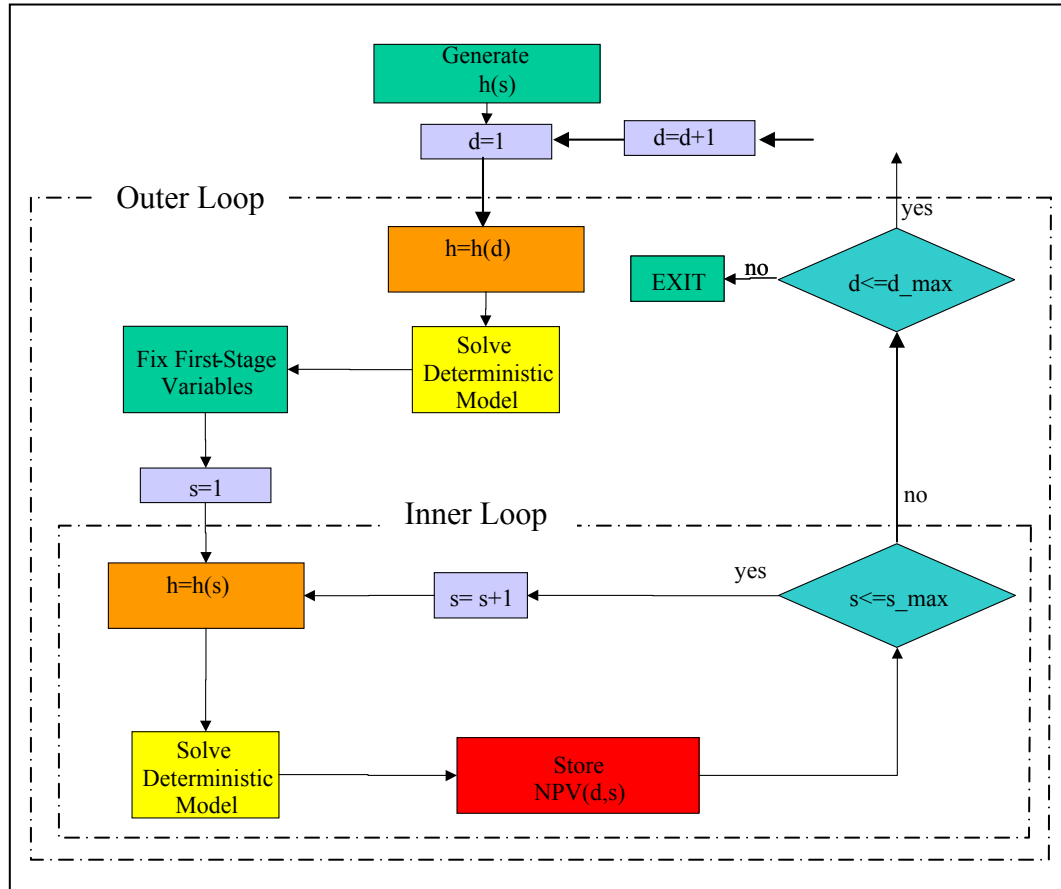
Two-Stage Stochastic Programming Using Regret Theory

NPV								
	s1	s2	s3	s4	s5	ENPV	Max	Min
d1	19.01	10.38	10.57	15.48	10.66	13.22	19.01	10.38
d2	11.15	14.47	8.87	20.54	10.58	13.12	20.54	8.87
d3	12.75	7.81	16.02	22.25	9.16	13.60	22.25	7.81
d4	5.41	9.91	12.63	32.02	8.08	13.61	32.02	5.41
d5	15.09	7.40	8.81	12.48	15.05	11.77	15.09	7.40
Max	19.01	14.47	16.02	32.02	15.05	13.61	32.02	10.38

Regret						
	s1	s2	s3	s4	s5	Max
d1	0.00	4.09	5.45	16.54	4.39	16.54
d2	7.86	0.00	7.15	11.48	4.47	11.48
d3	6.26	6.66	0.00	9.77	5.89	9.77
d4	13.60	4.56	3.39	0.00	6.97	13.60
d5	3.92	7.07	7.21	19.54	0.00	19.54
Min						9.77



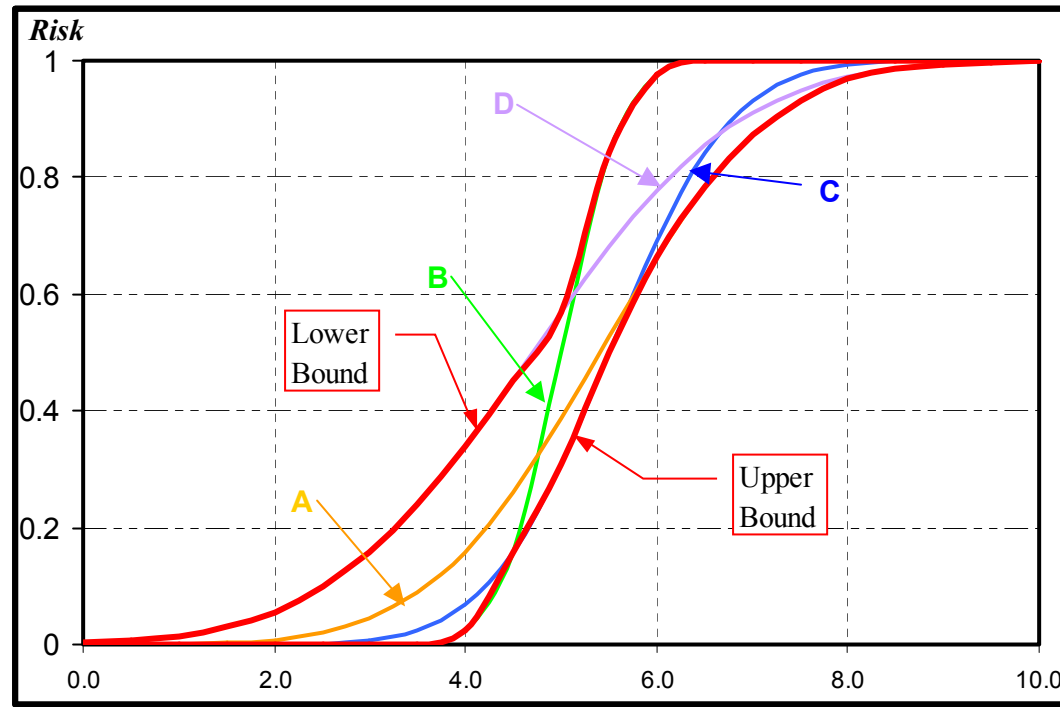
SAMPLING ALGORITHM



This generates several solutions



UPPER AND LOWER BOUNDS

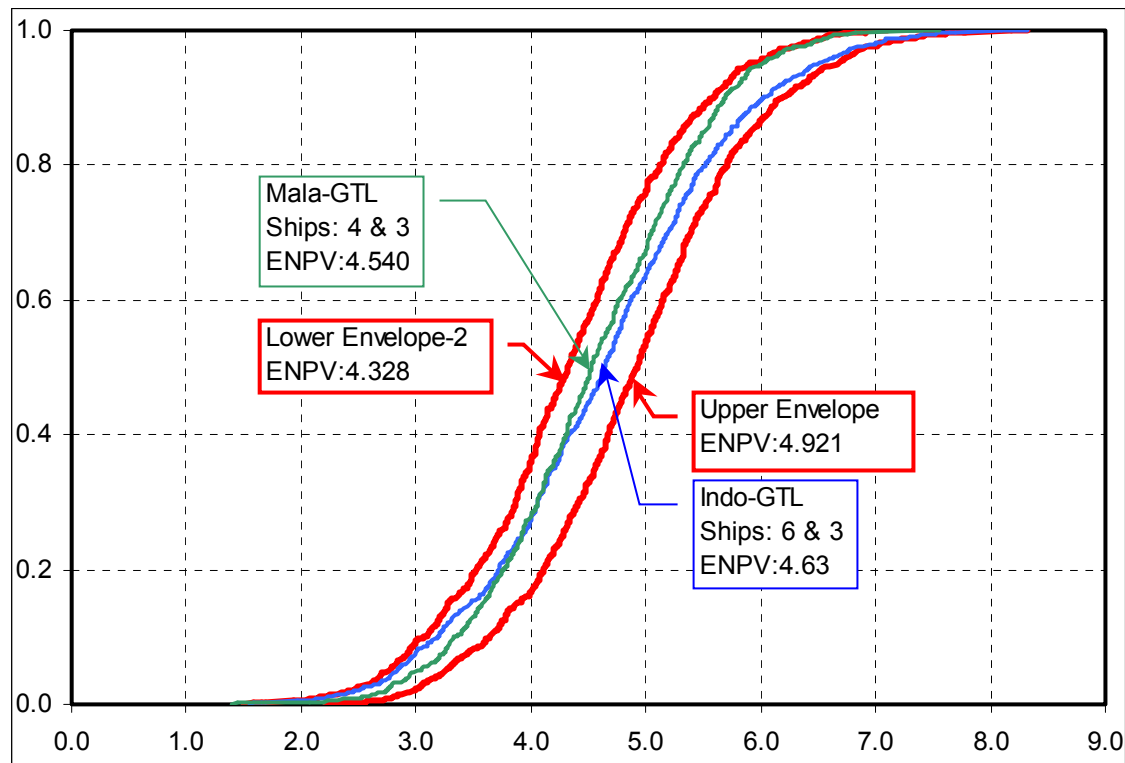


*This is very useful because it allows nice decomposition,
That is, **there is no need** to solve the full stochastic problem*



UPPER AND LOWER BOUNDS

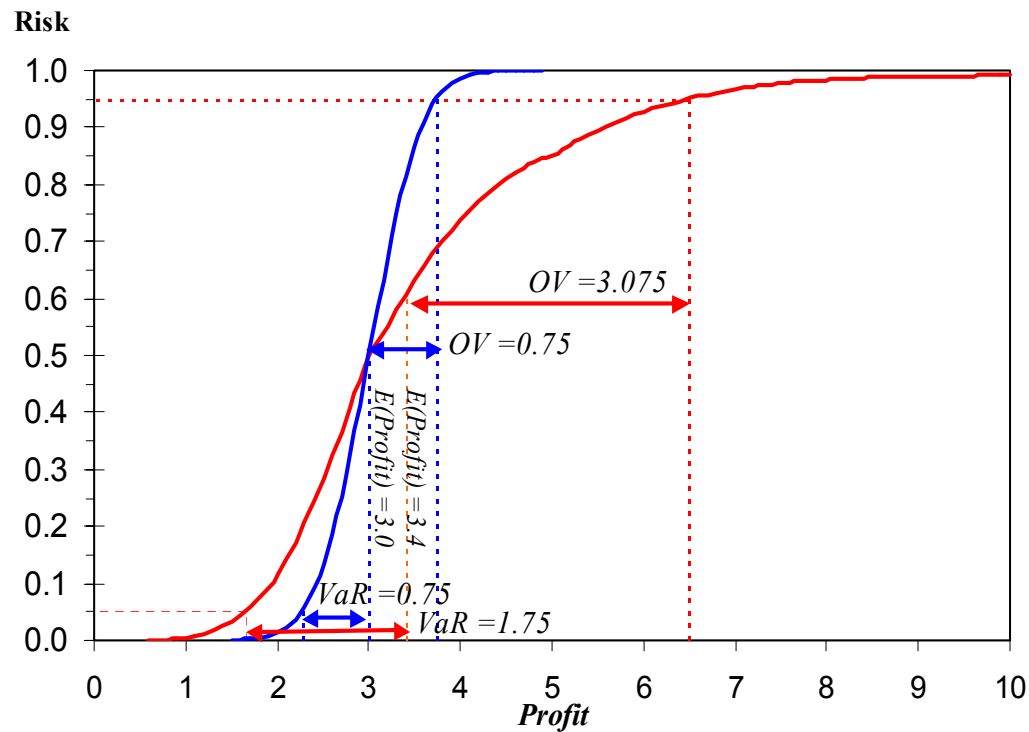
Example: Gas Commercialization in Asia





UPSIDE POTENTIAL

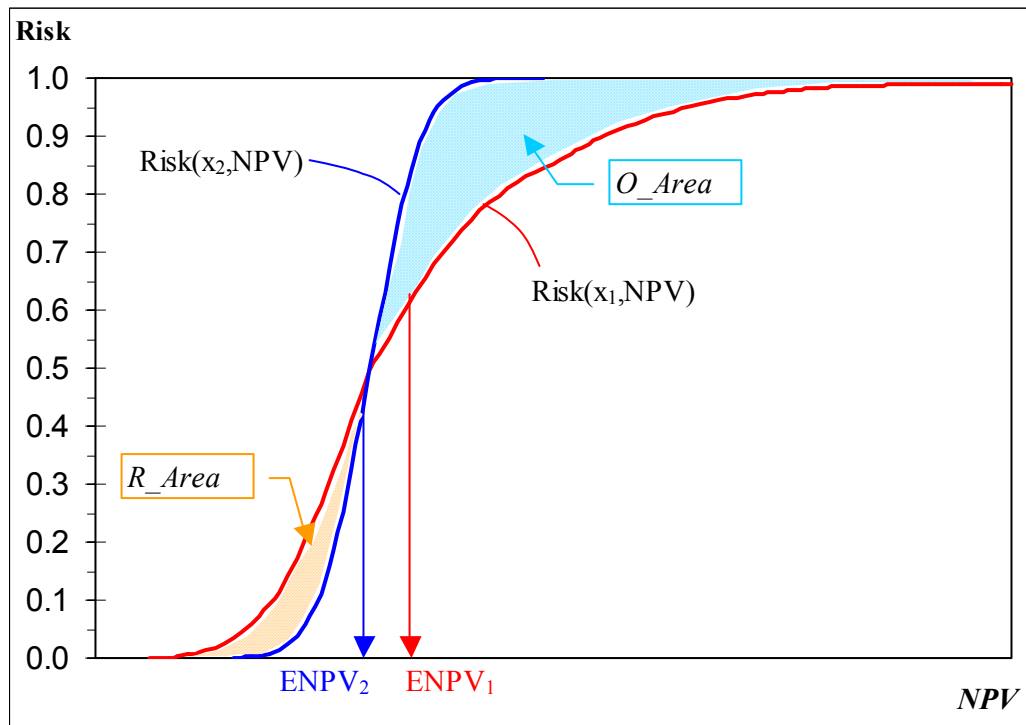
Point measure for the upside





AREA RATIO

Comparison measure



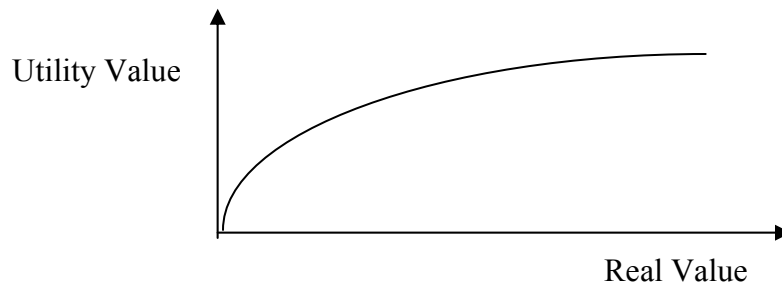


UTILITY THEORY

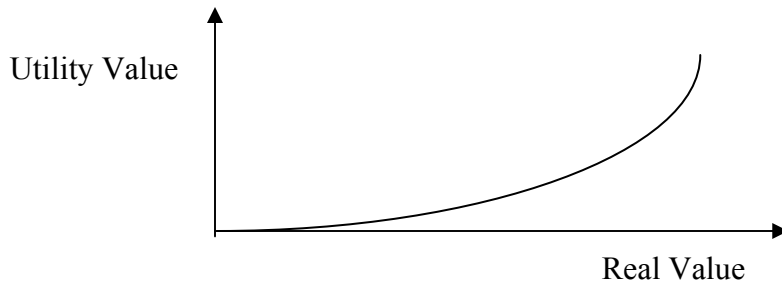
Utility Functions

Money does not always have the same value for a company

- ❖ A Risk Averse Decision Maker values more low profits than large ones



- ❖ A Risk Taker values more high profits

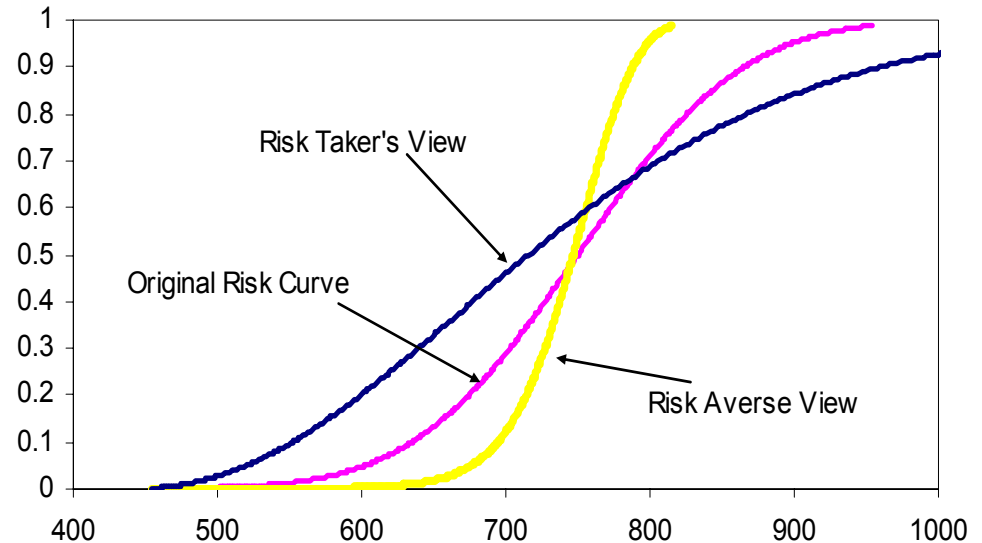
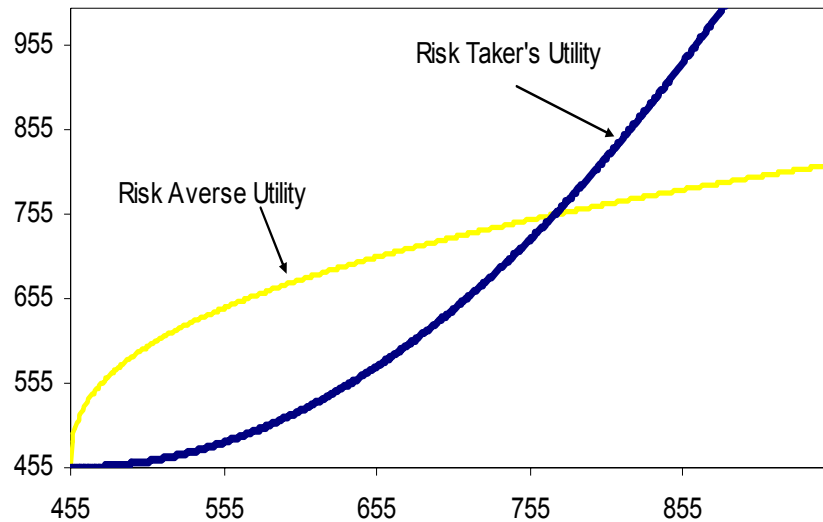




UTILITY THEORY

Use Utility Value instead of real profit for evaluation

Effect on Risk Curves





CONCLUSIONS

- **Regret Analysis can help in identifying good solutions (It can also fail)**
- **The sampling Algorithm is an important tool to identify upper bounds and good solutions.**
- **The upper potential is important to be considered.**

References

- **Riggs J. L. *Economic Decision Models for Engineers and Managers*. McGraw Hill, NY, 1968**
- **Aseeri A. and M. Bagajewicz. *New Measures and Procedures to Manage Financial Risk with Applications to the Planning of Gas Commercialization in Asia*. Computers and Chemical Engineering**