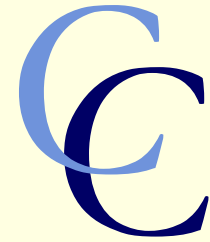


## Cartilage Tissue Engineering

Emily Burdett  
Victoria Froude

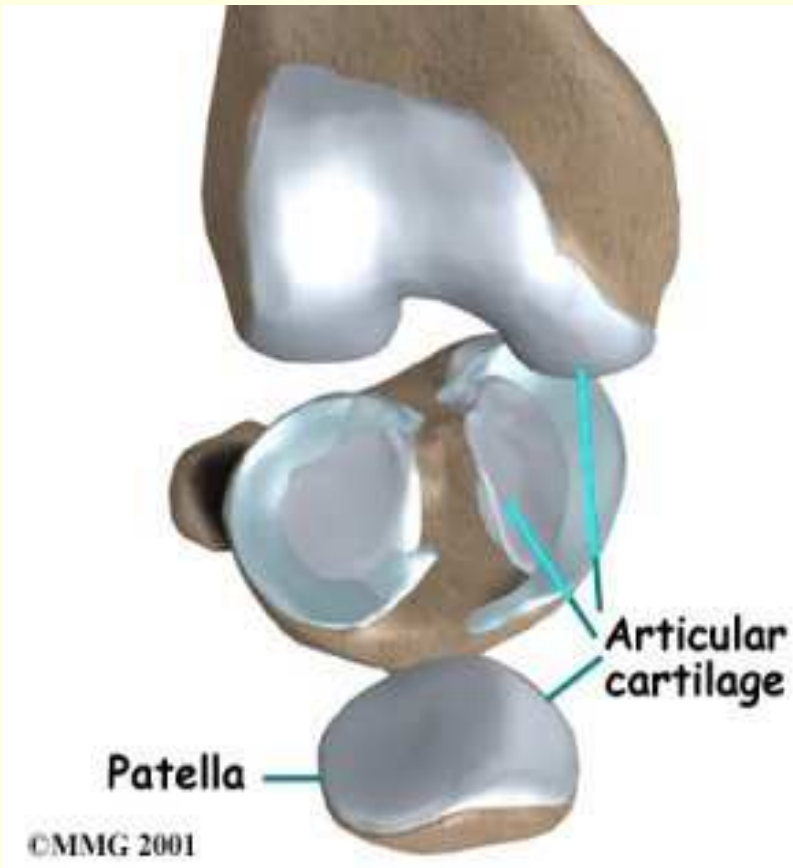
May 2, 2006

# Overview



- Cartilage damage in the knee is a major problem
- We present a novel tissue engineering technique for repairing cartilage damage with autologous chondrocyte cells
- Mathematical modeling can be useful to help predict implant behavior
- The FDA approval process and product pricing were modeled in order to evaluate risk

# Cartilage

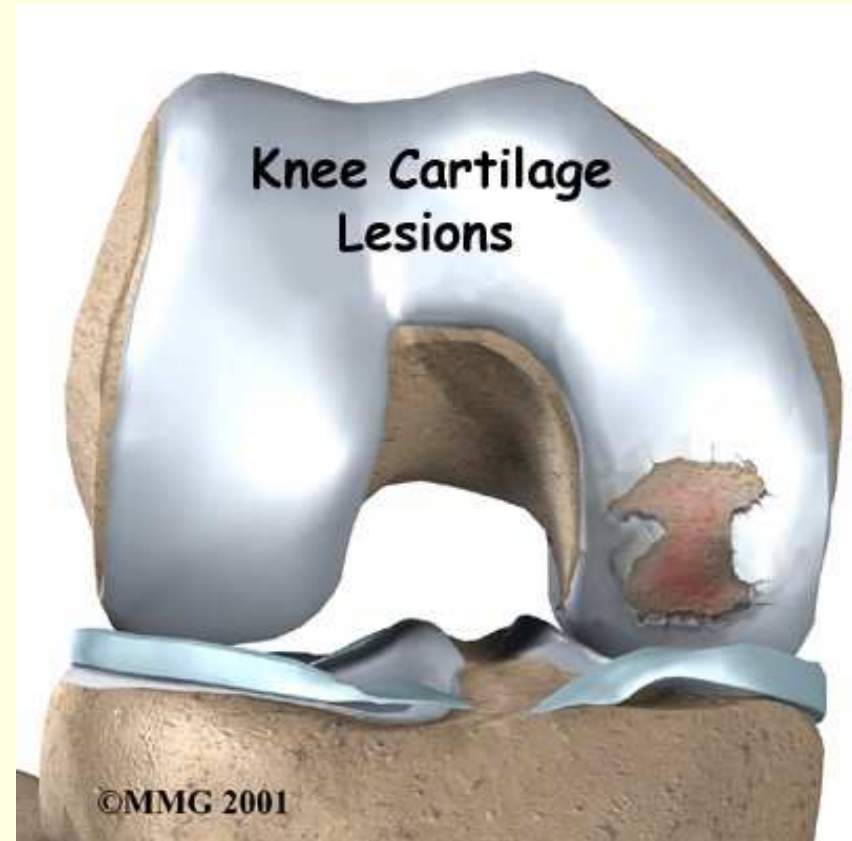


- Connective tissue found in all joints
- Functions as cushioning and support
- Cartilage is composed of chondrocytes, collagen, and proteoglycans.
- Articular cartilage is found in the knee joint.
  - Strongest type of cartilage

# Cartilage Damage



- Tears and holes develop in cartilage due to injury and stress.
- No vascular system is present throughout the cartilage to initiate repair after damage.
- Damage develops in cartilage and extends into the underlying bone.

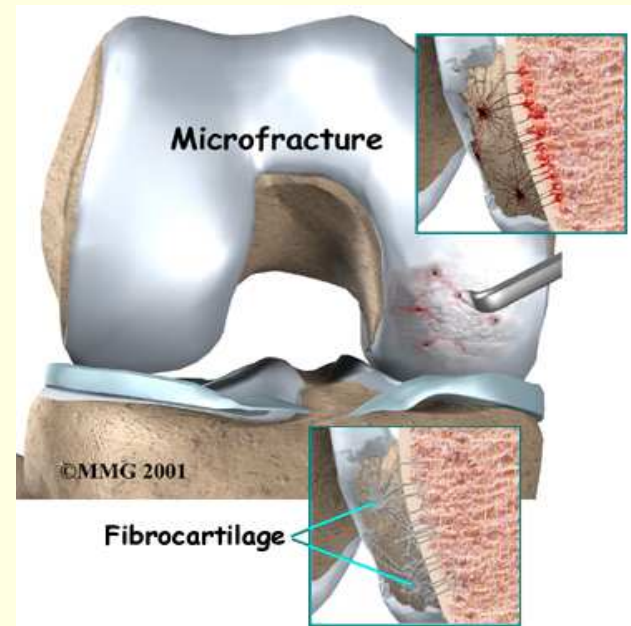


[http://www.orthogastonia.com/index.php/fuseaction/patient\\_ed.topicdetail/TopicID/a93dd54cd3d79c0d8bedae1537bc7659/area/17](http://www.orthogastonia.com/index.php/fuseaction/patient_ed.topicdetail/TopicID/a93dd54cd3d79c0d8bedae1537bc7659/area/17)

# Reparative Surgeries

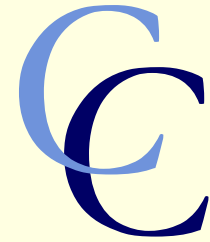


- Inflict further damage to initiate the healing response.
  - New tissue does not have the required mechanical strength.
  - Results are temporary.

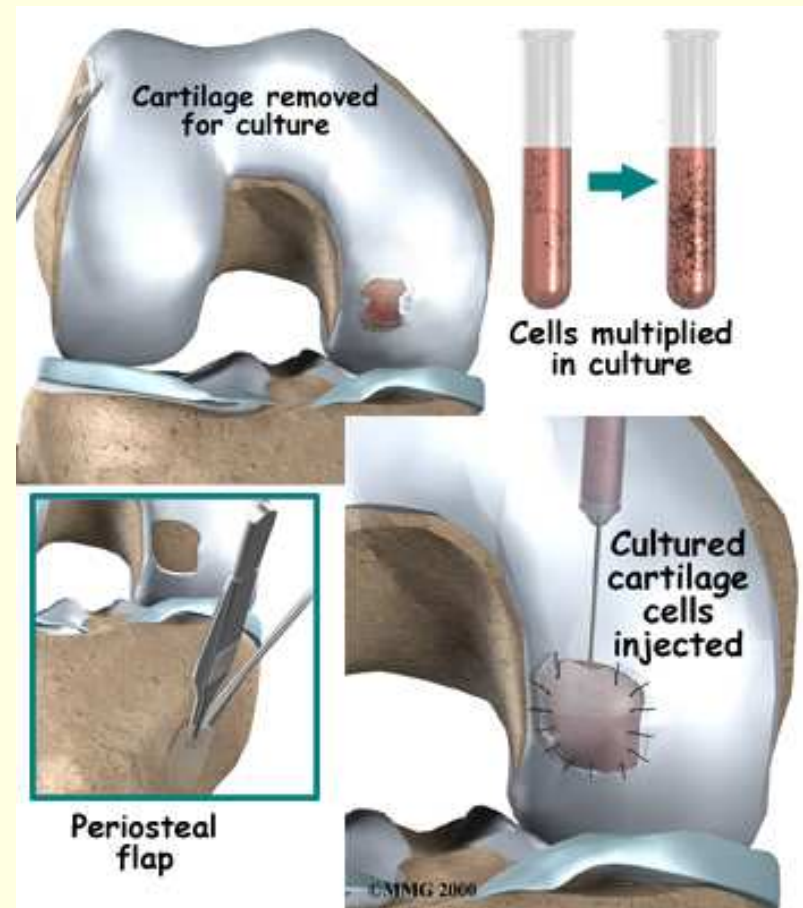


[http://www.orthogastonia.com/index.php/fuseaction/patient\\_ed.topicdetail/TopicID/a93dd54cd3d79c0d8bedae1537bc7659/area/17](http://www.orthogastonia.com/index.php/fuseaction/patient_ed.topicdetail/TopicID/a93dd54cd3d79c0d8bedae1537bc7659/area/17)

# Restorative Surgeries



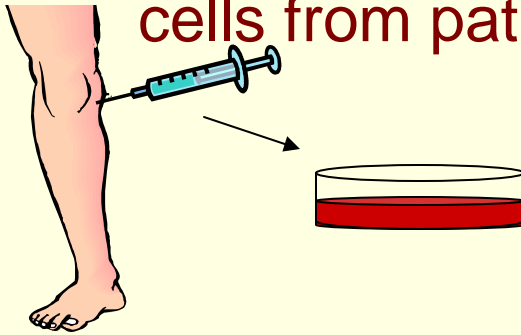
- Replace cartilage with cells or donor tissue.
  - Invasive
  - Lack reliability
  - High risk of initiating an immune response
  - Cells migrate from damage site



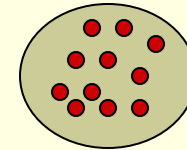
# Our Solution



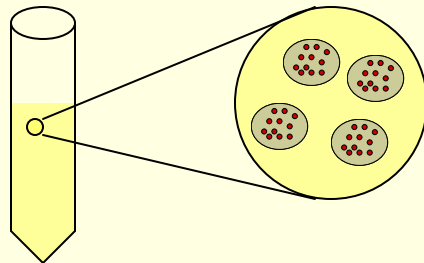
1) Harvest and proliferate cells from patient



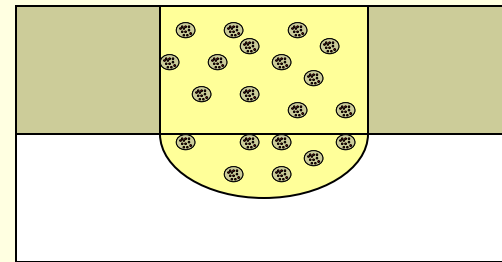
2) Embed cells in gelatin microcapsules



3) Suspend capsules in crosslinkable polymer



4) Inject polymer into defect and crosslink *in situ*



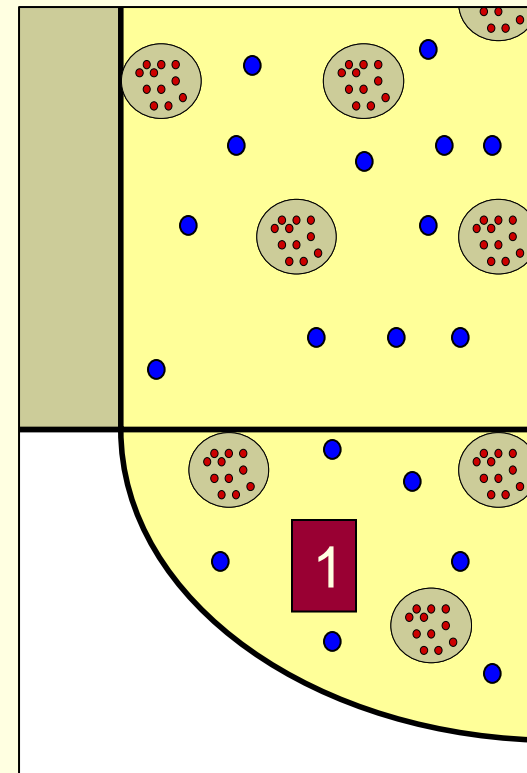
After crosslinking, microcapsules will release cells. Over time, polymer will degrade and cells will produce new tissue

# Cartilage Repair



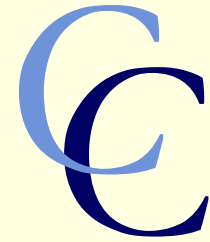
## 1. Bone replacement:

- Made of poly(propylene fumarate) (PPF) combined with  $\beta$ -TCP particles
- Seeded with mesenchymal stem cells taken from the patient's bone marrow.
- N-vinylpyrrolidinone serves as a crosslink and benzoyl peroxide initiates crosslinking upon injection



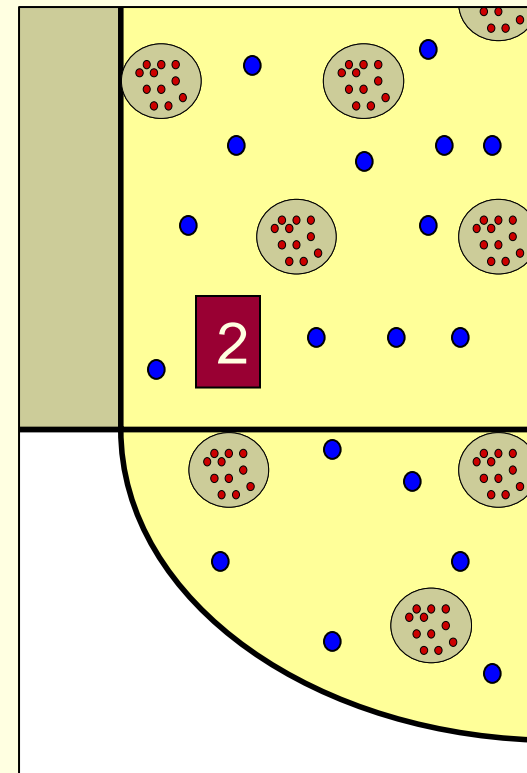


# Cartilage Repair

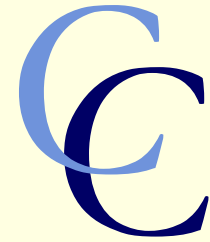


## 2. Cartilage Replacement:

- Made of a copolymer containing PPF and poly(ethylene glycol) (PPF-co-EG)
- Seeded with chondrocytes taken from a non-load bearing joint
- Undergoes the same crosslinking reaction as the bone replacement

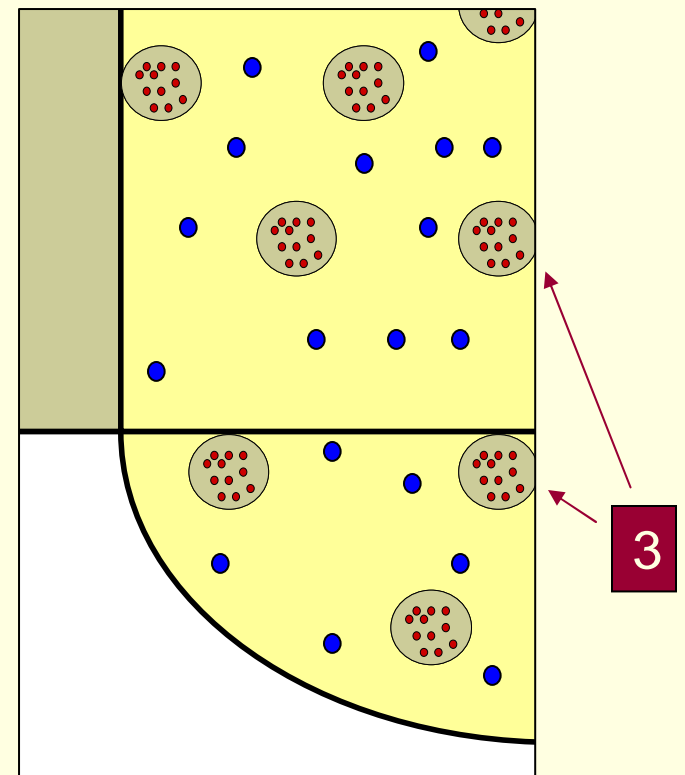


# Cartilage Repair

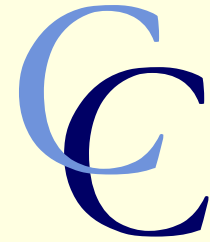


## 3. Cell Microcapsules

- Microcapsules will contain porcine gelatin and DMEM cell culture media
- Surface will be crosslinked using DSP to prevent reverse gelation of microparticles during PPF crosslinking

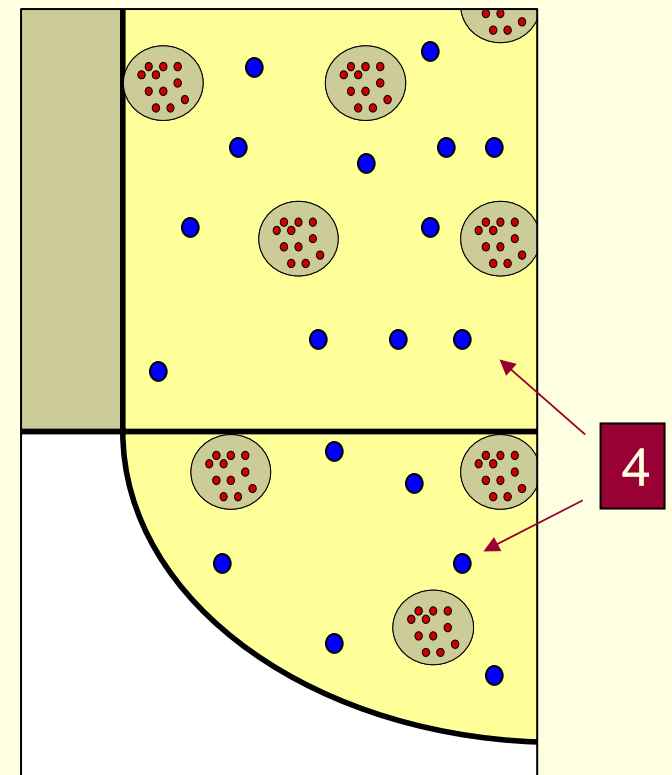


# Cartilage Repair

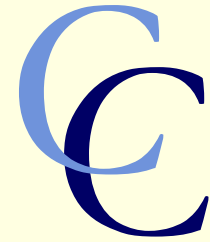


## 4. Growth Factors

- PLGA microparticles containing growth factors will also be suspended in the polymer
- These will release growth factors slowly throughout tissue regeneration to promote cell growth and activity

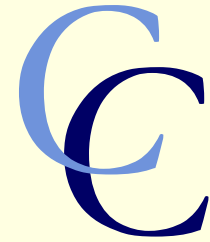


# Technical Models



- Mathematical modeling of aspects of this procedure will decrease the amount of experimentation needed and decrease the risk associated with lack of knowledge.
- Aspects that can be modeled:
  - Heat Transfer
  - Mechanical Strength / Porosity
  - Polymer Degradation

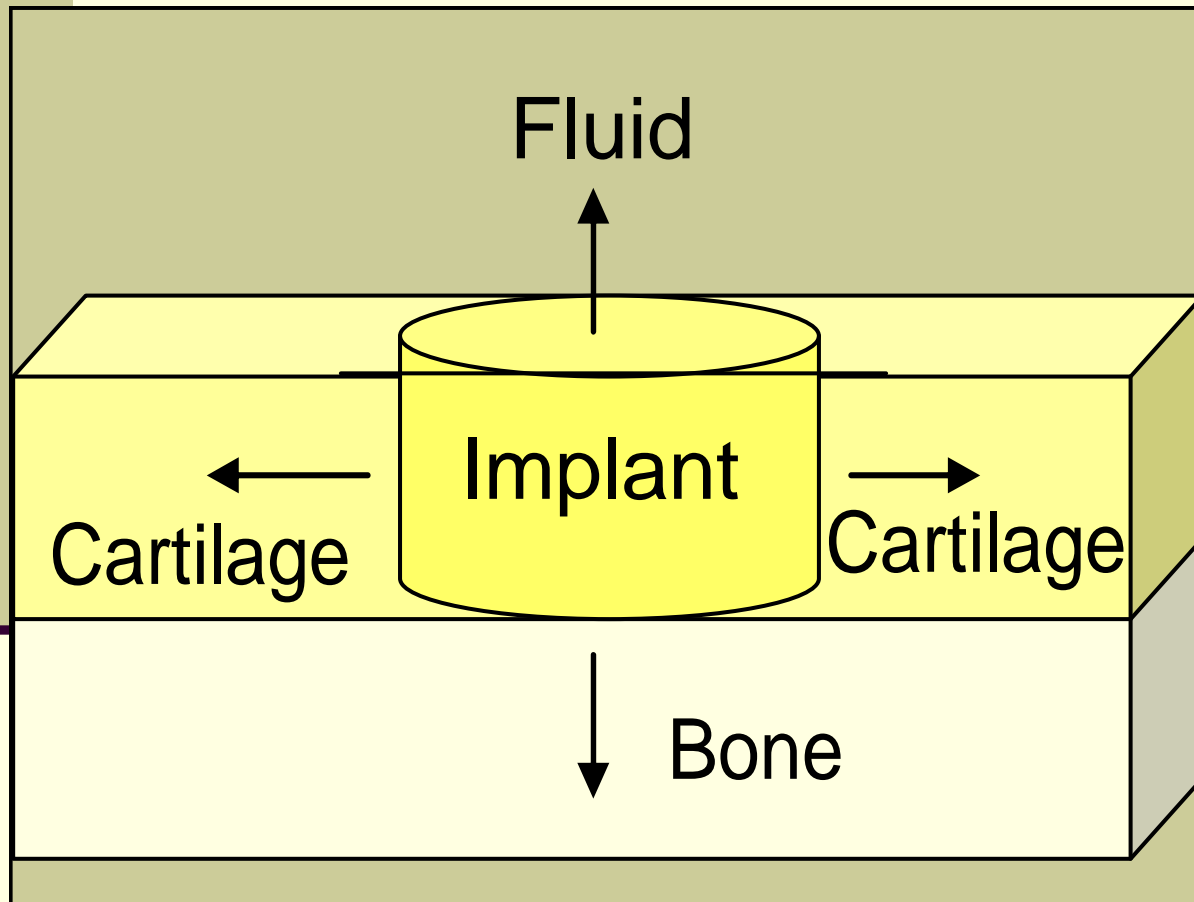
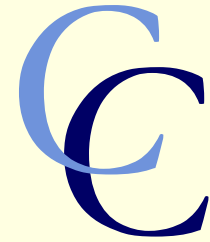
# Heat Transfer



- When cell suspension polymerizes *in vivo*, heat is produced.
- This causes the temperature of the polymer construct to increase.
- Excessive temperatures can kill the cells before they can begin to proliferate and create tissue.
- Will increased polymer temperatures allow enough cell survival for tissue growth?



# Heat Transfer



Inside Implant

$$\alpha_1 \frac{\partial T}{\partial t} = \nabla^2 T + \dot{q}(t)$$

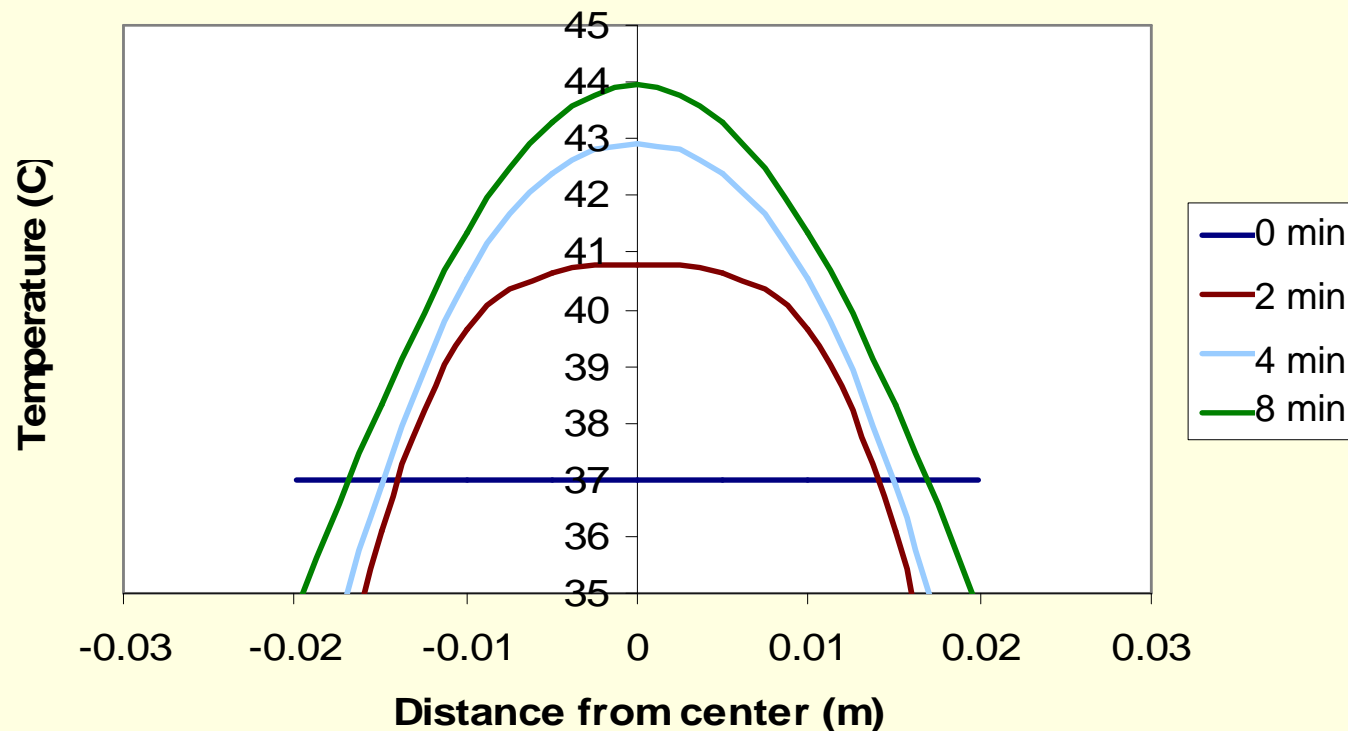
Outside Implant

$$\alpha_2 \frac{\partial T}{\partial t} = \nabla^2 T$$

# Heat Transfer



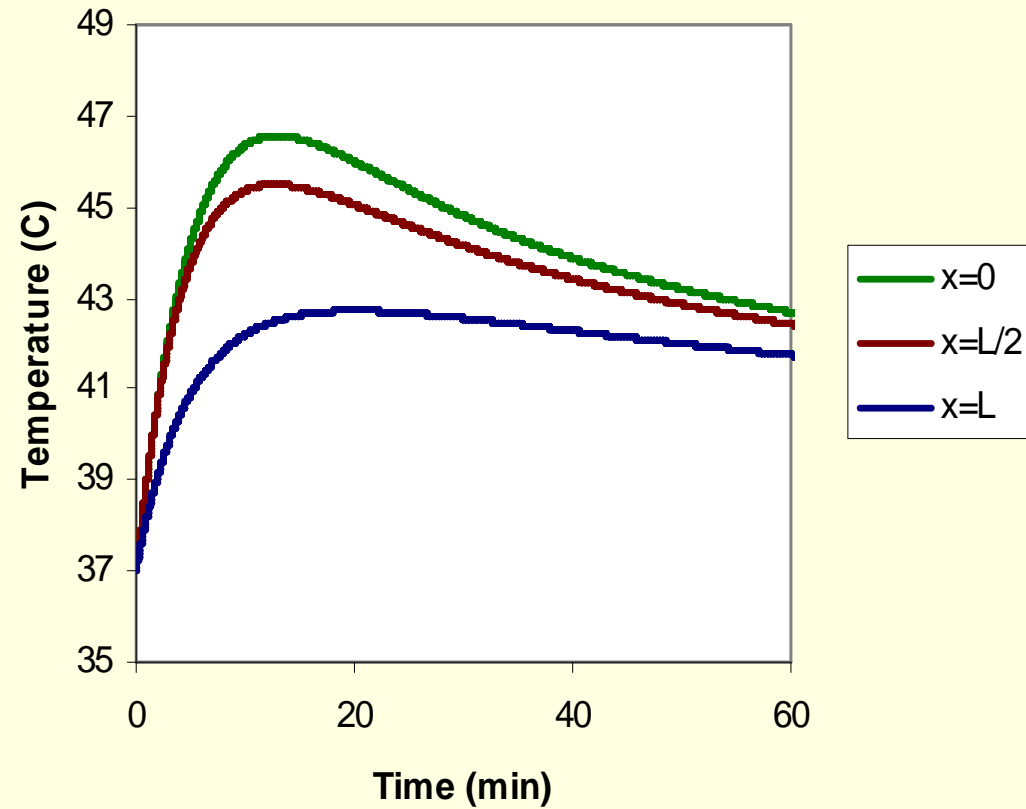
- First attempt: 1-D Analytical Solution
- Solution of inner equation is not consistent with boundary conditions.



# Heat Transfer



- Second Attempt: find 1-D solution numerically using finite differences
- Temperature raises to almost  $47^{\circ}\text{C}$  and stays above  $40^{\circ}\text{C}$  for several hours
- This would cause significant cell death

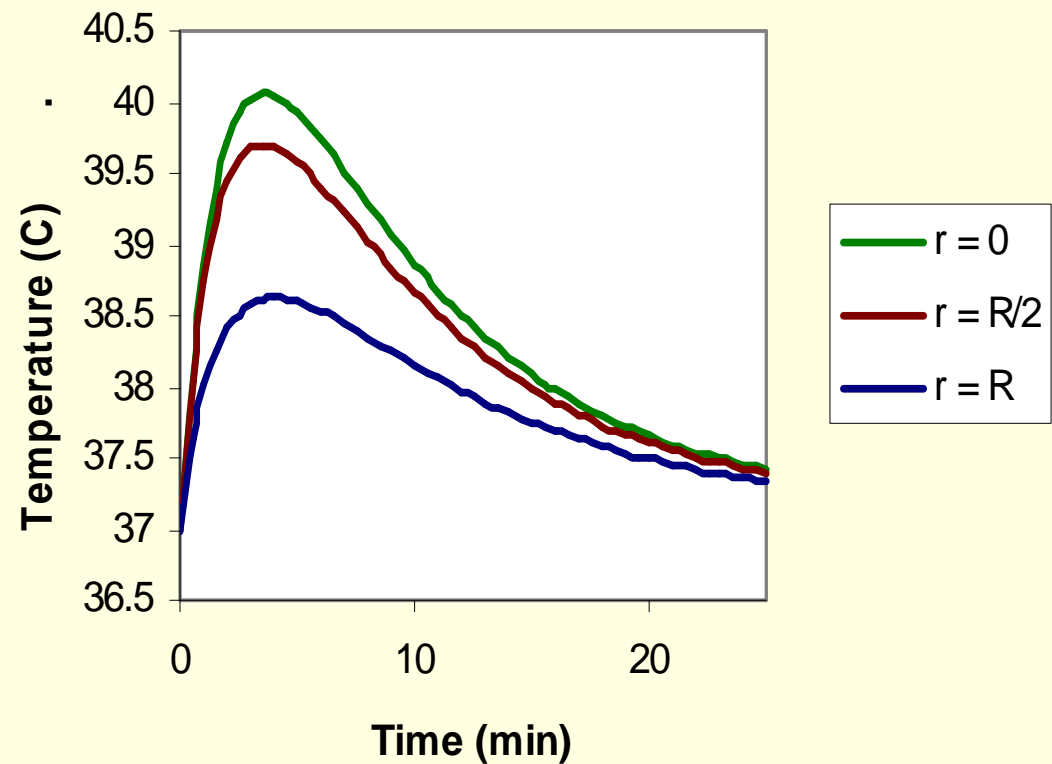




# Heat Transfer



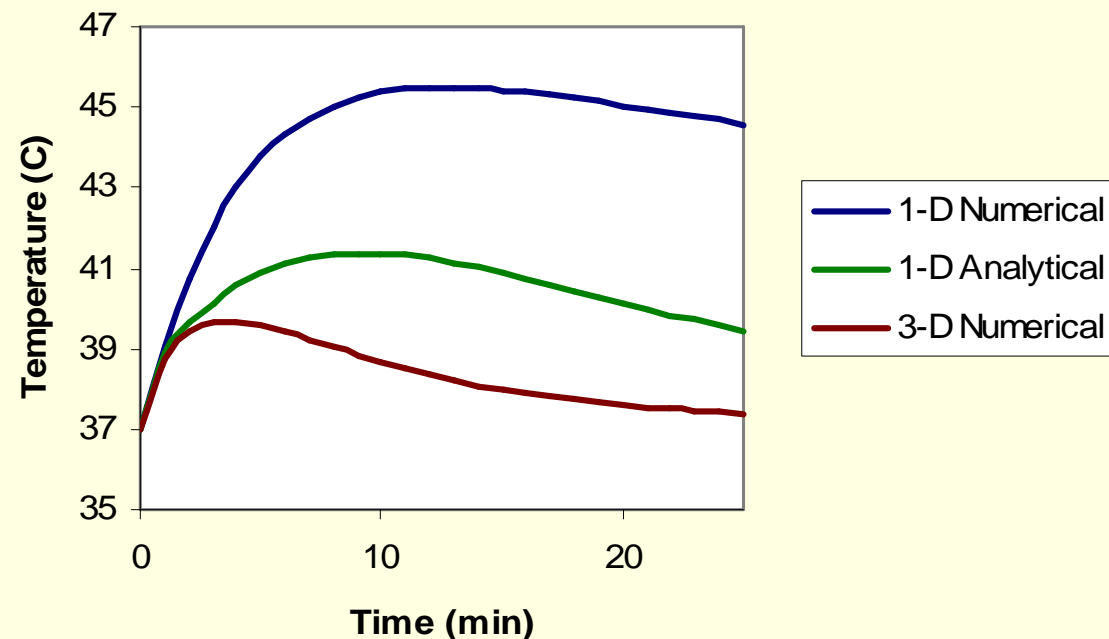
- Third Attempt: Find 3-D solution in cylindrical coordinates using finite differences
- Temperature only increases to 40 C at the Center of the Implant
- This temperature increase will cause minimal cell death



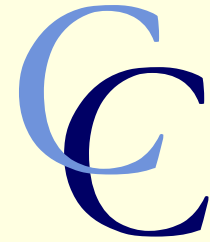
# Heat Transfer



- Comparison between methods
- 1-D Models do not consider heat lost through the top and bottom of the implant

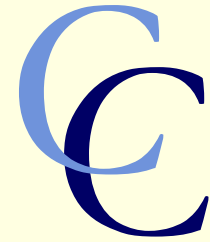


# Heat Transfer



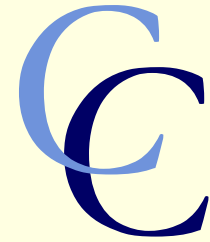
- 
- Model shows that temperature increase will not cause significant cell death.
  - This prediction gives a starting point for experiments in cell seeding.
  - The model saves us money and time that would otherwise be used to find these results experimentally

# Mechanical Strength



- Proper mechanical strength will allow for better recovery for the patient
- Natural compressive strength
  - Bone ~ 5 MPa
  - Cartilage ~ 0.4 – 1.4 MPa
- Variables affecting construct strength throughout device life:
  - Cross-linking density
  - Porosity
  - Degradation and cell growth

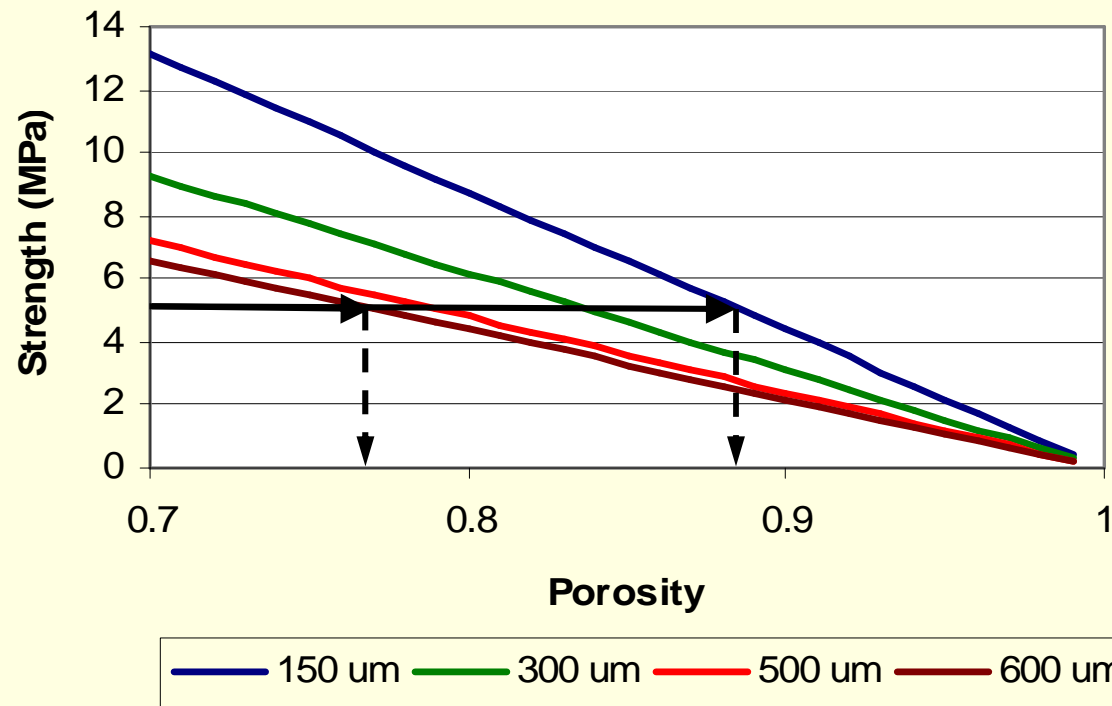
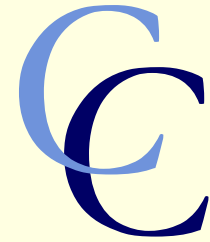
# Porosity



- Void space is necessary to create pathways for nutrient and waste movement.
- Porosity affects compressive strength of the material
  - Percent porosity of material
  - Size and morphology of pores
- Atzeni equation developed for hardened pastes with spherical pores.
  - Empirical constant is necessary

$$\sigma = K \frac{\sigma_0 (1 - p)}{\sqrt{r_m}}$$

# PPF/ $\beta$ -TCP Porosity



$$\sigma = 4.3 \frac{\sigma_0 (1-p)}{\sqrt{r_m}}$$

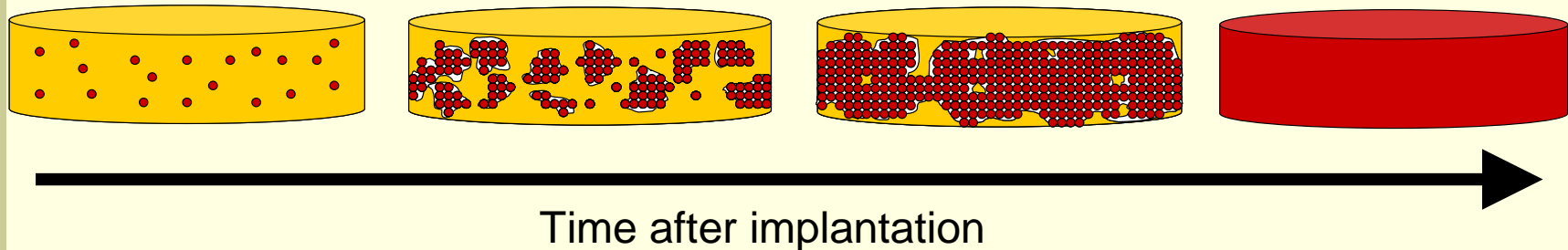
- Natural bone has a compressive strength of 5 MPa.
- Bone substitute could have a porosity over 75% based on this model.

# PPF-co-EG Porosity



- Polymer matrix forms a hydrogel, which has natural void space.
  - Dependent on cross-linking density
- Shown to have adequate diffusion of nutrients, waste, and large proteins.
- Diffusion of nutrients and mechanical strength are affected by the cross-linking density of the polymer.

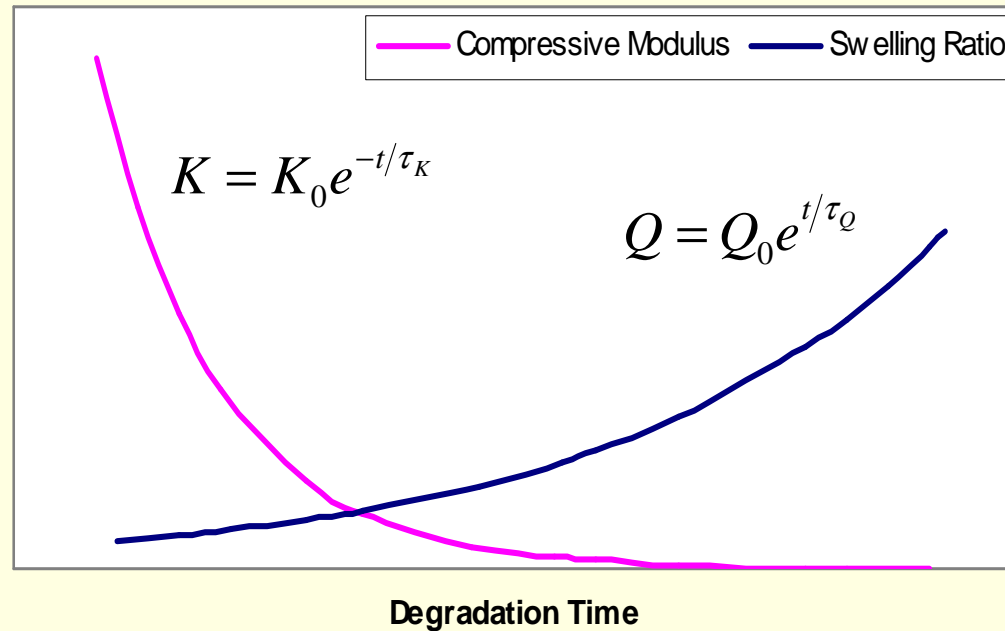
# Construct degradation



- Degradation occurs by hydrolysis of PPF bonds.
- Pseudo-first order kinetics because water concentration is relatively constant.
- Degradation decreases cross-linking density
  - Decreases compressive strength
  - Increases swelling ratio



# Degradation Effects



- As degradation increases, polymer loses strength
- Degradation rate is dependent on initial cross-linking density
- Cell growth must replace degraded polymer to maintain strength.

# Modeling

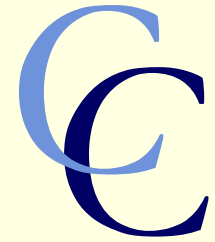


- We now have a better idea of which experiments must be done in order to make this process work.
- Overall, numerical models like this help to reduce cost and more accurately quantify risk...

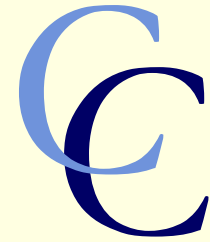


# Risk Analysis

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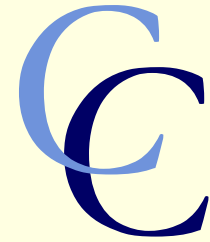


# Need for Risk Analysis



- New technologies include an incredible amount of risk
  - 5 of every 5,000 medical technologies that enters the FDA approval process enters human clinical testing.
  - Only 1 of those 5 technologies will eventually be approved for the medical market.
- On average, it takes 15 years for the approval process.
- It takes approximately \$360 million for a new technology to reach the public.

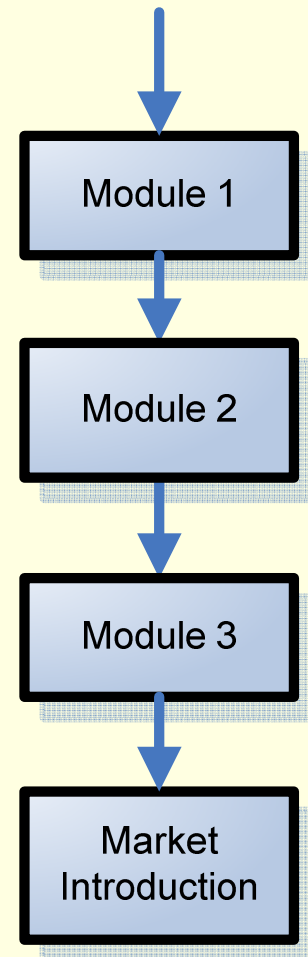
# FDA Approval



- 
- Necessary before the use of any medical device.
  - Experiments determine the positive and negative affects of the treatment.
    - Lab scale testing
    - Animal testing
    - Human clinical trials
  - Application can be filed in a traditional or modular form.

# Modular FDA Approval

- Modules are determined based on assessment of needed experiments.
- Request approval at the end of each module
- Failure within a module does not indicate total product failure
  - Data appendices can be sent in after approval was requested.
- Project can be abandoned after failure at any module.



# FDA Approval



- Module 1 – Laboratory testing
  - Bench scale testing
  - Basic material properties
  - Initial optimization of construct
- Module 2 – Non-clinical animal studies
  - Defining surgical procedure
  - Biocompatibility and toxicity studies
  - Further optimization of construct
- Module 3 – Human clinical trials
  - Mechanical strength and integrity
  - Long-term *in vivo* results

# Assessing Pathways

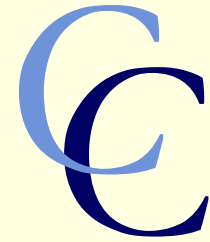


- Each step has an associated time, cost, and probability.
- To assess the FDA process, estimations of where failures will occur must be made.
- Number of failures allowable within a pathway will greatly affect the risk assessment.
- Probabilities of success would increase if
  - Pre-FDA testing is completed
  - More experiments are performed
  - Advance and accurate modeling is available



# Pre-FDA Trials

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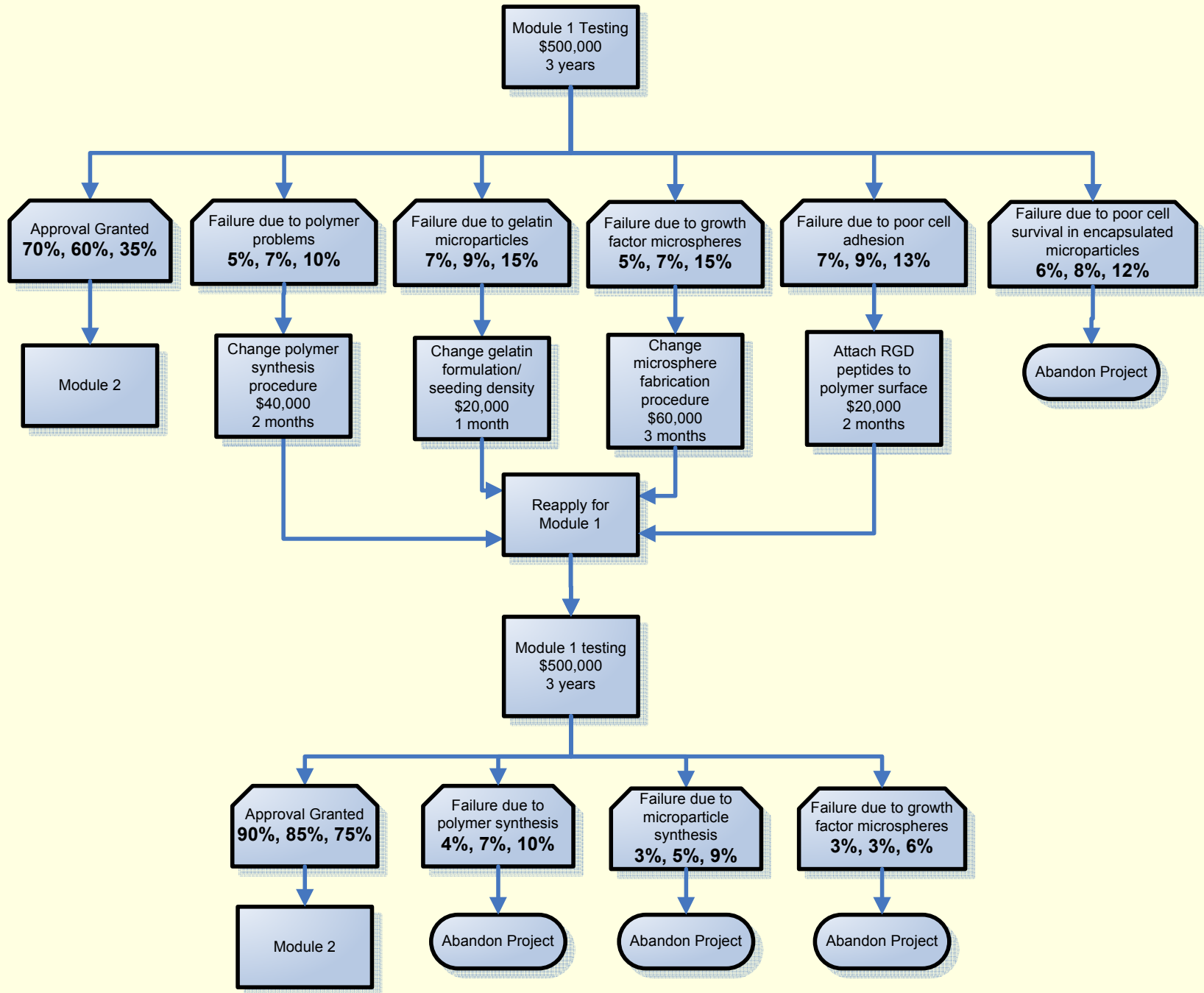
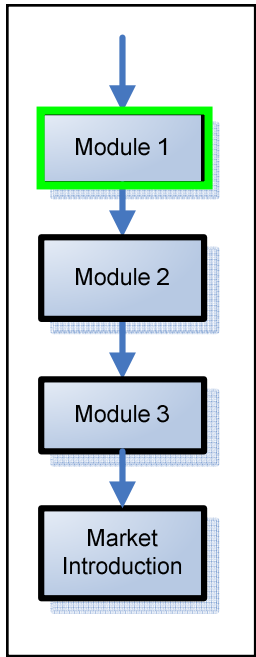
- Reduces the chance of early failure
- Abandon or change project based on results
- Predict necessity of more expensive experiments and optimizations
- Increases accuracy of risk analysis

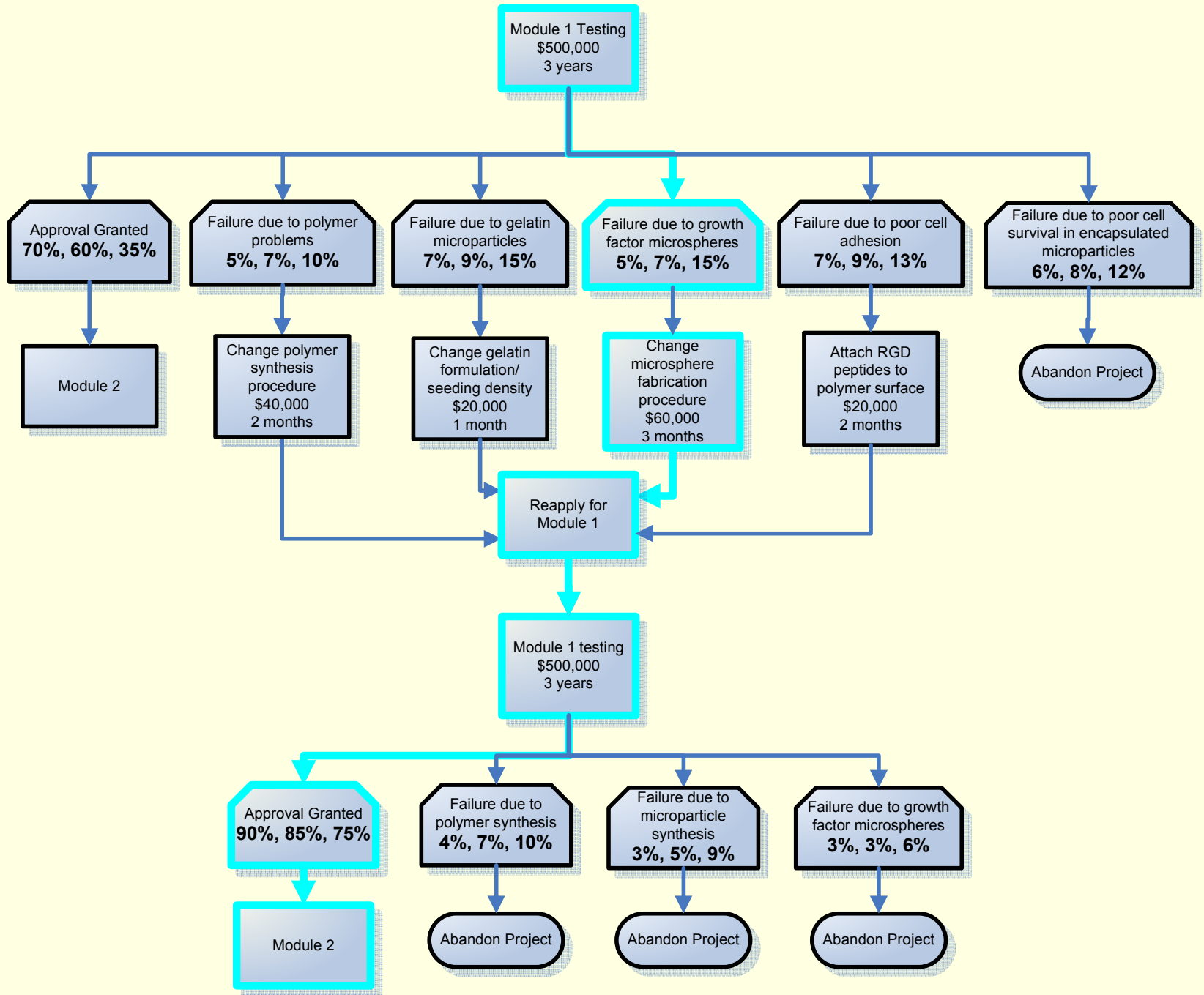
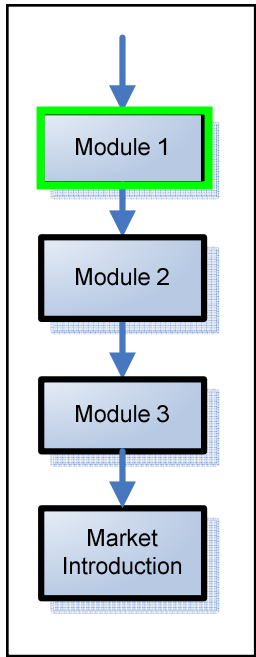
# Business Decisions

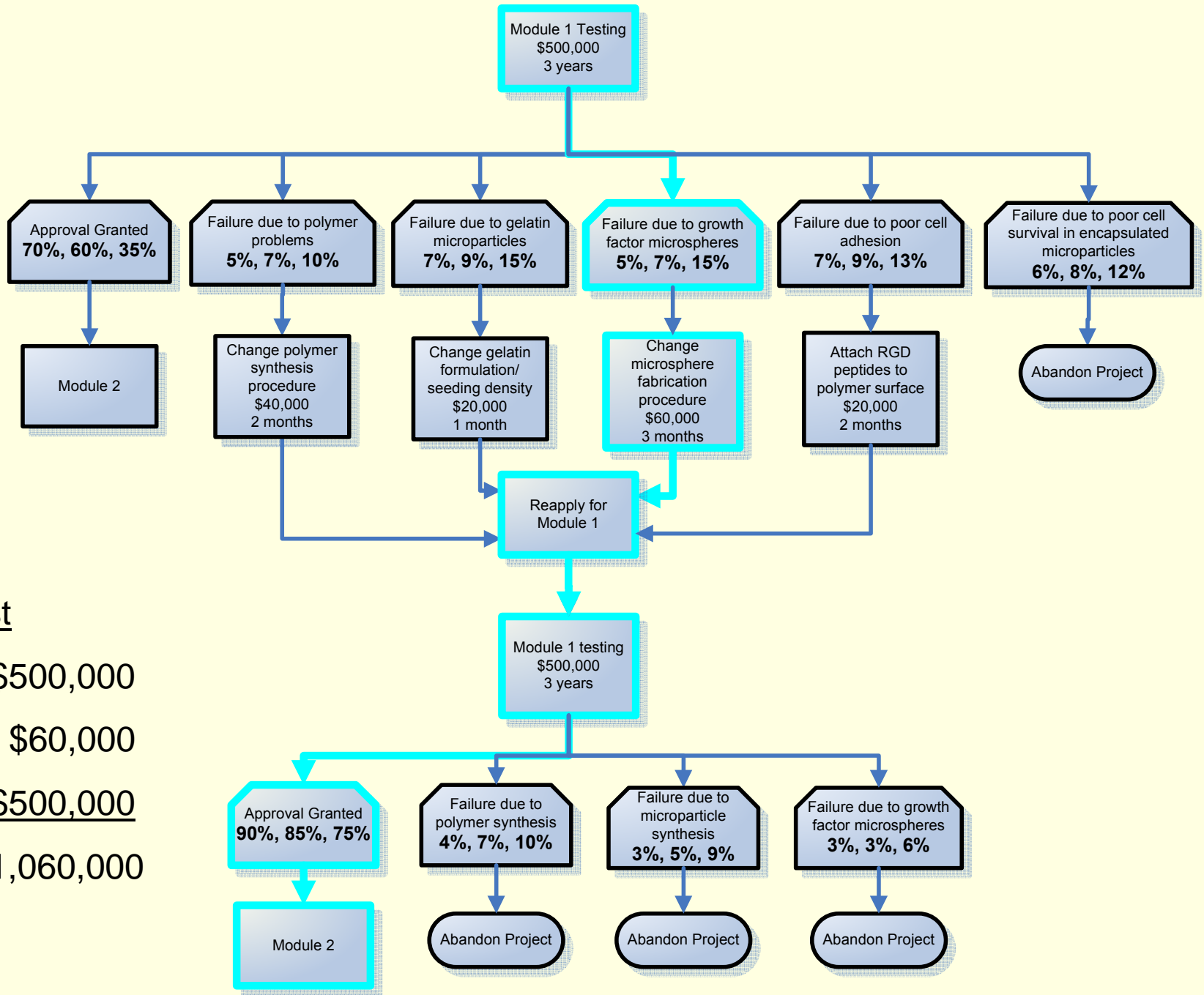
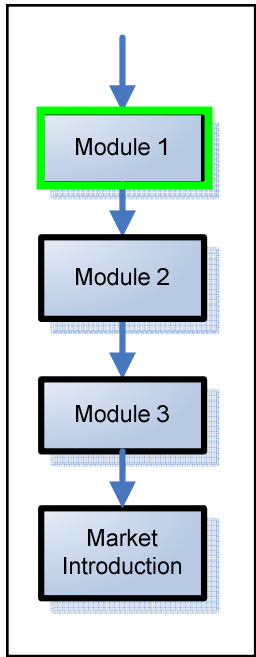


<b>First Stage Decisions:</b>	<b>Second Stage Decisions:</b>
Number of experiments	Product price
Number of workers	Advertising Costs
Number of Allowable Failures	Production facility location and size

- We will find risk associated with several first stage scenarios – it is assumed that second stage decisions can be made later for optimum performance







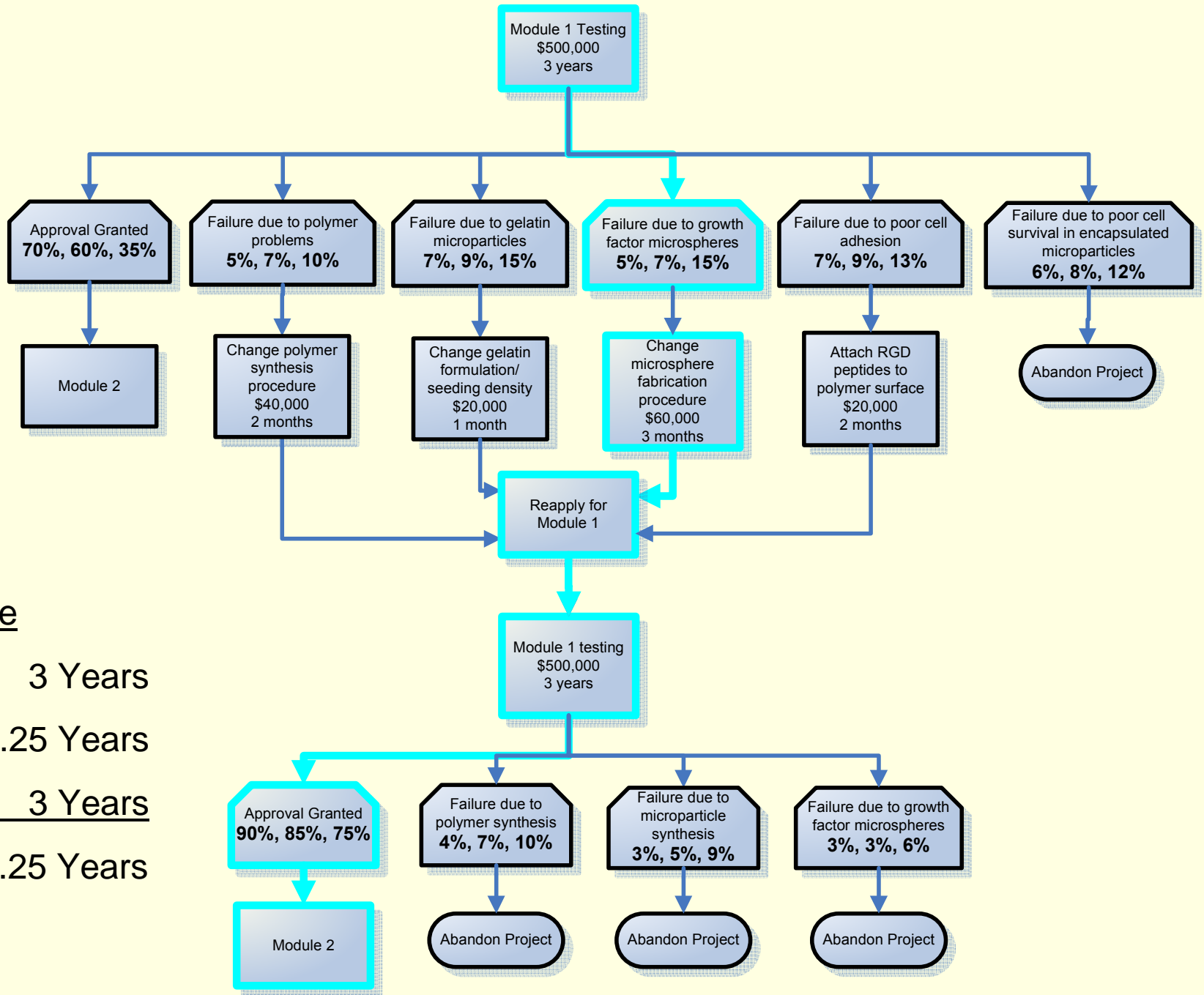
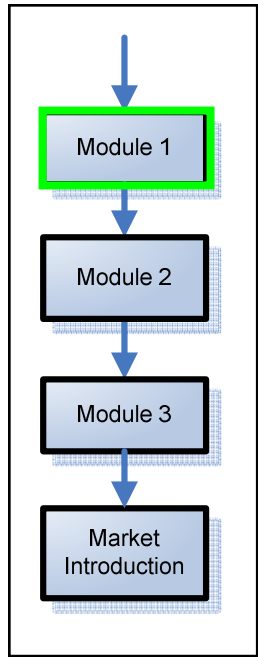
Cost

= \$500,000

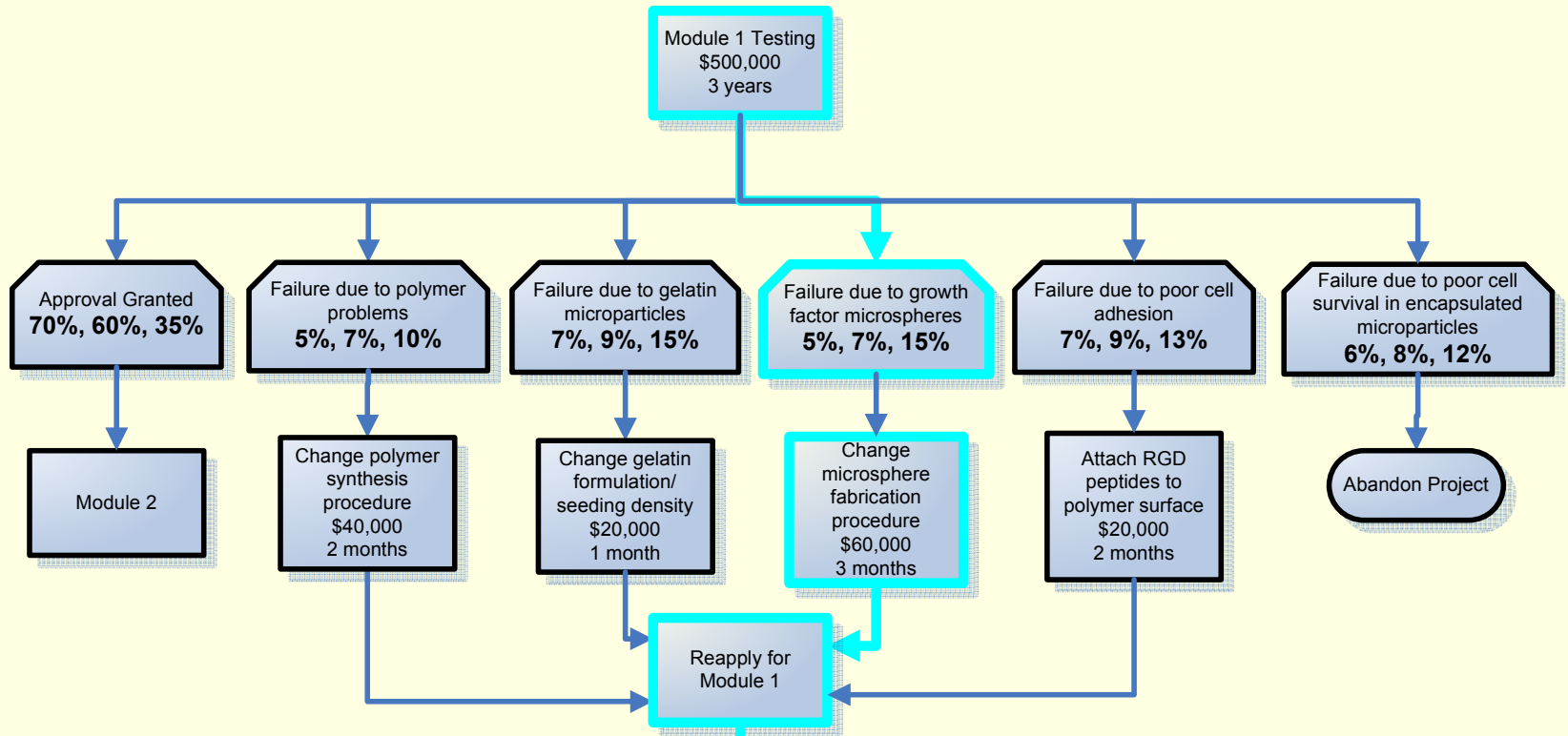
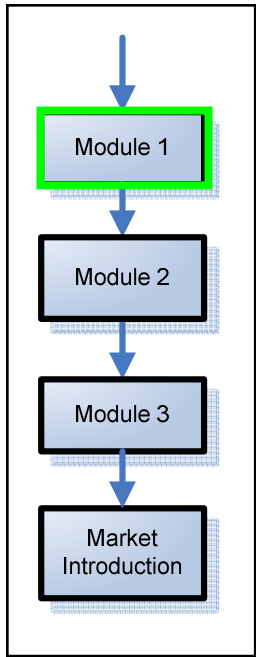
+ \$60,000

+ \$500,000

\$1,060,000



Time  
 = 3 Years  
 + 0.25 Years  
 + 3 Years  
 6.25 Years

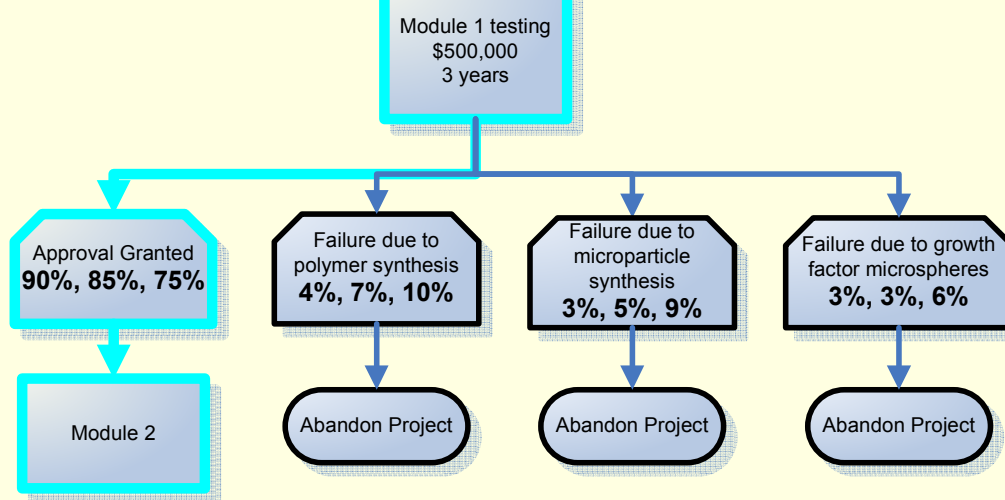


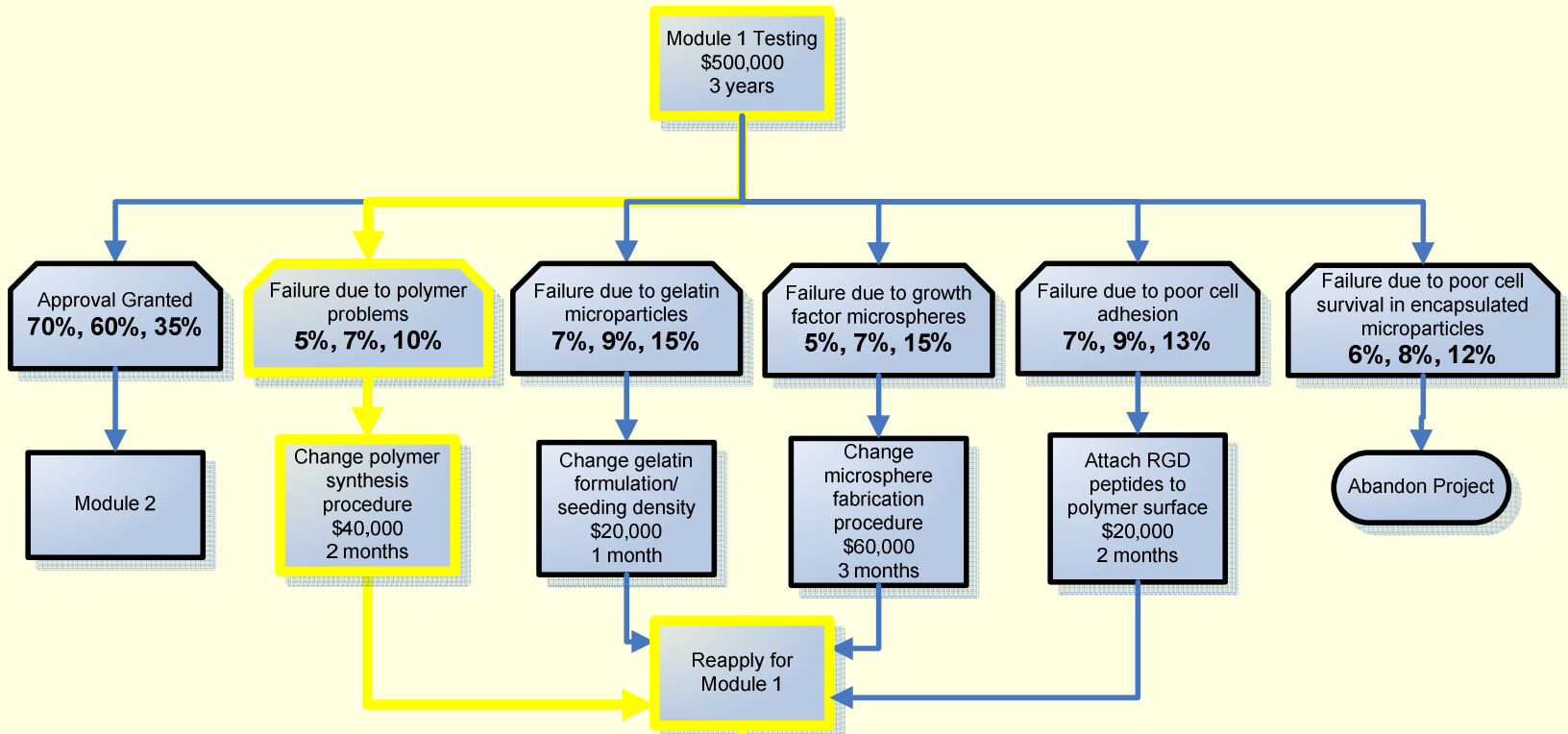
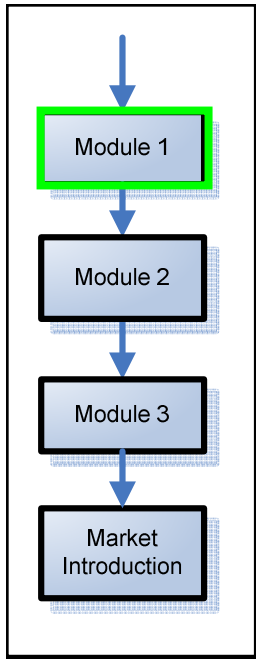
Probability

= 0.05

x 0.90

0.045





Cost

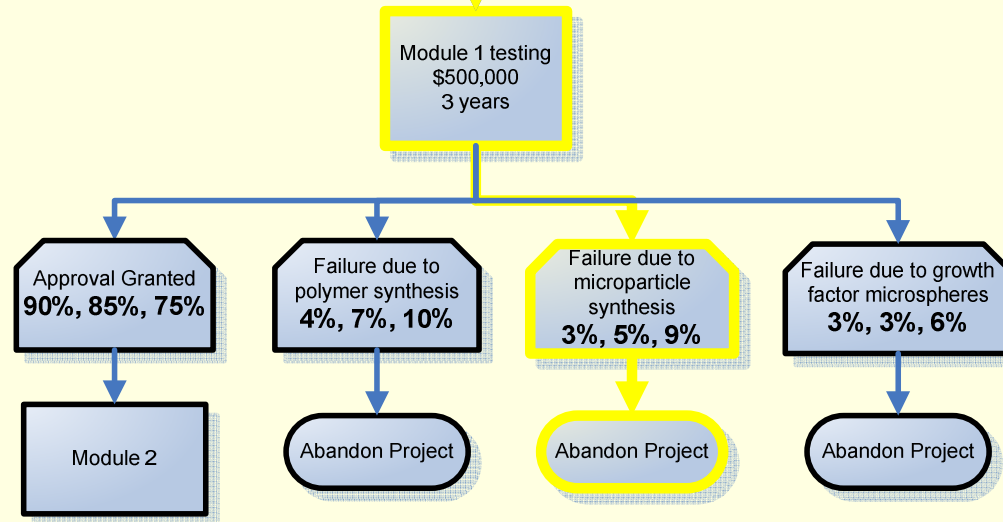
\$1,060,000

Time

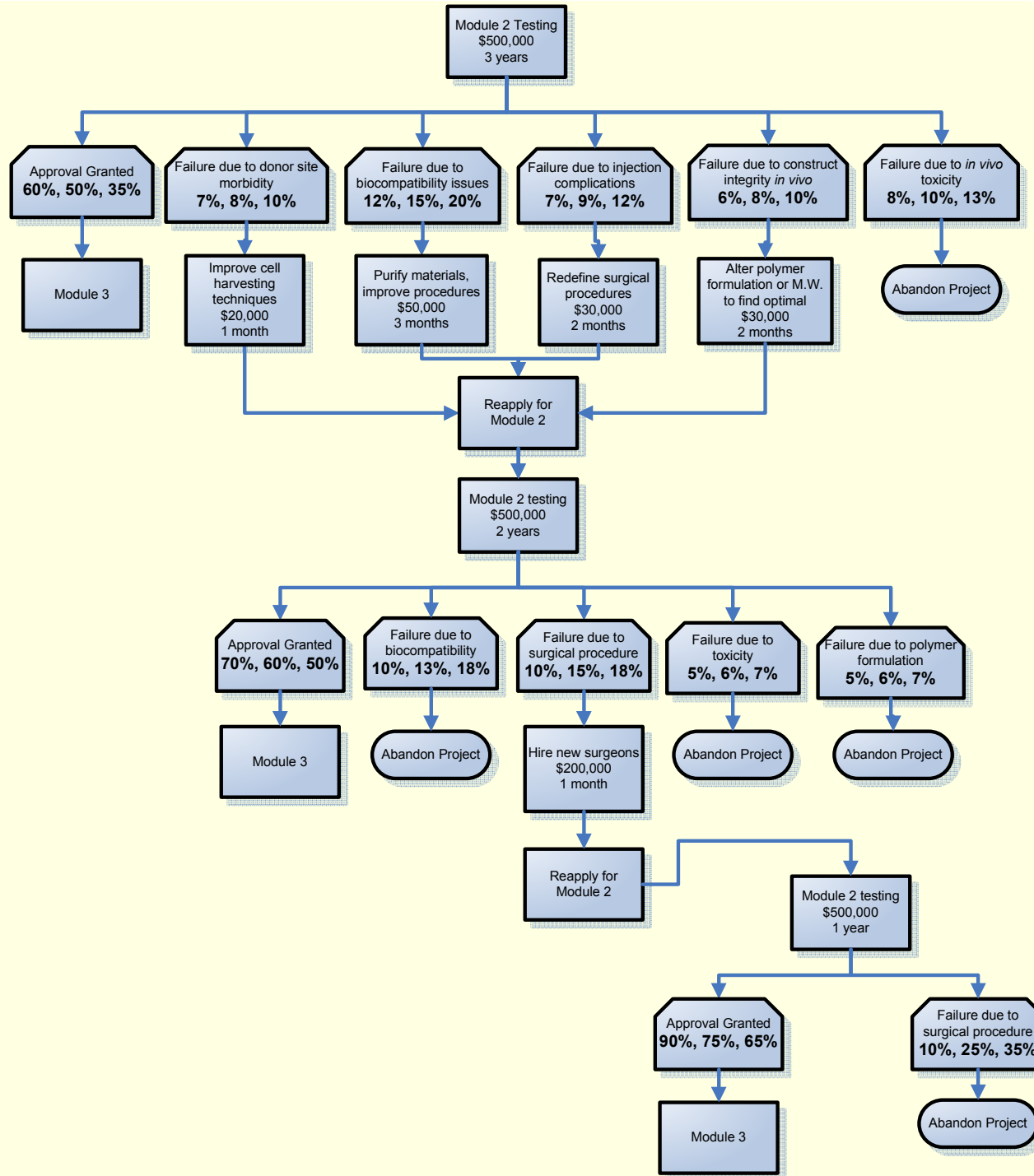
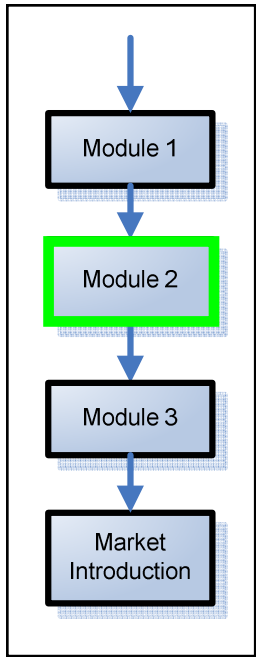
6.25 Years

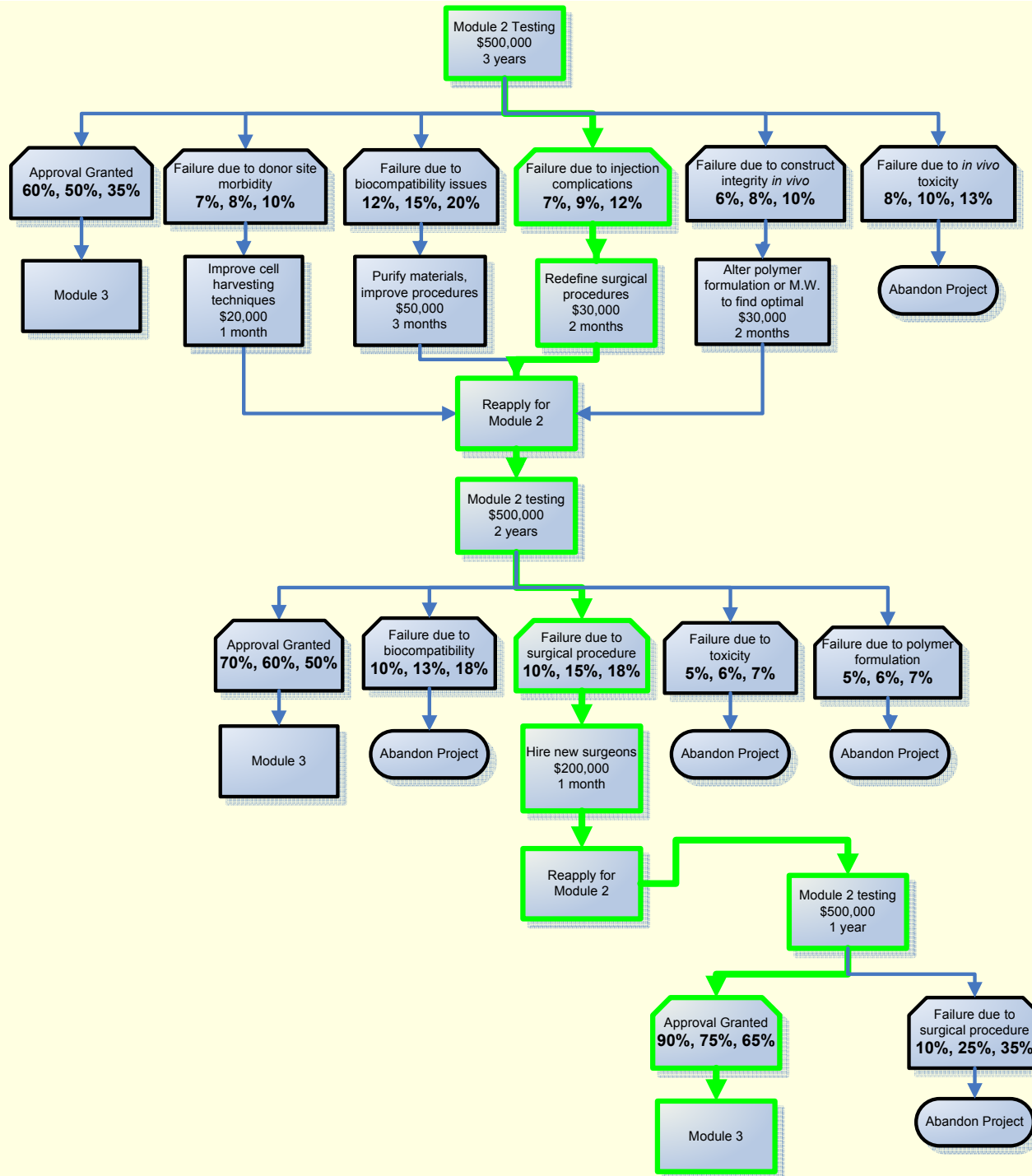
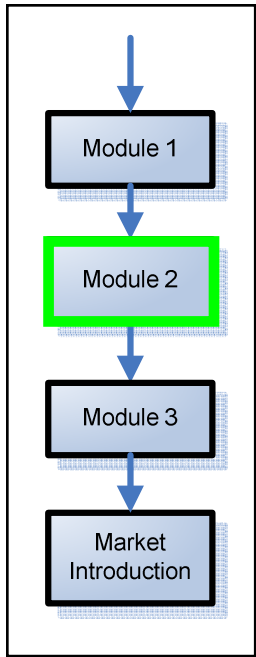
Probability

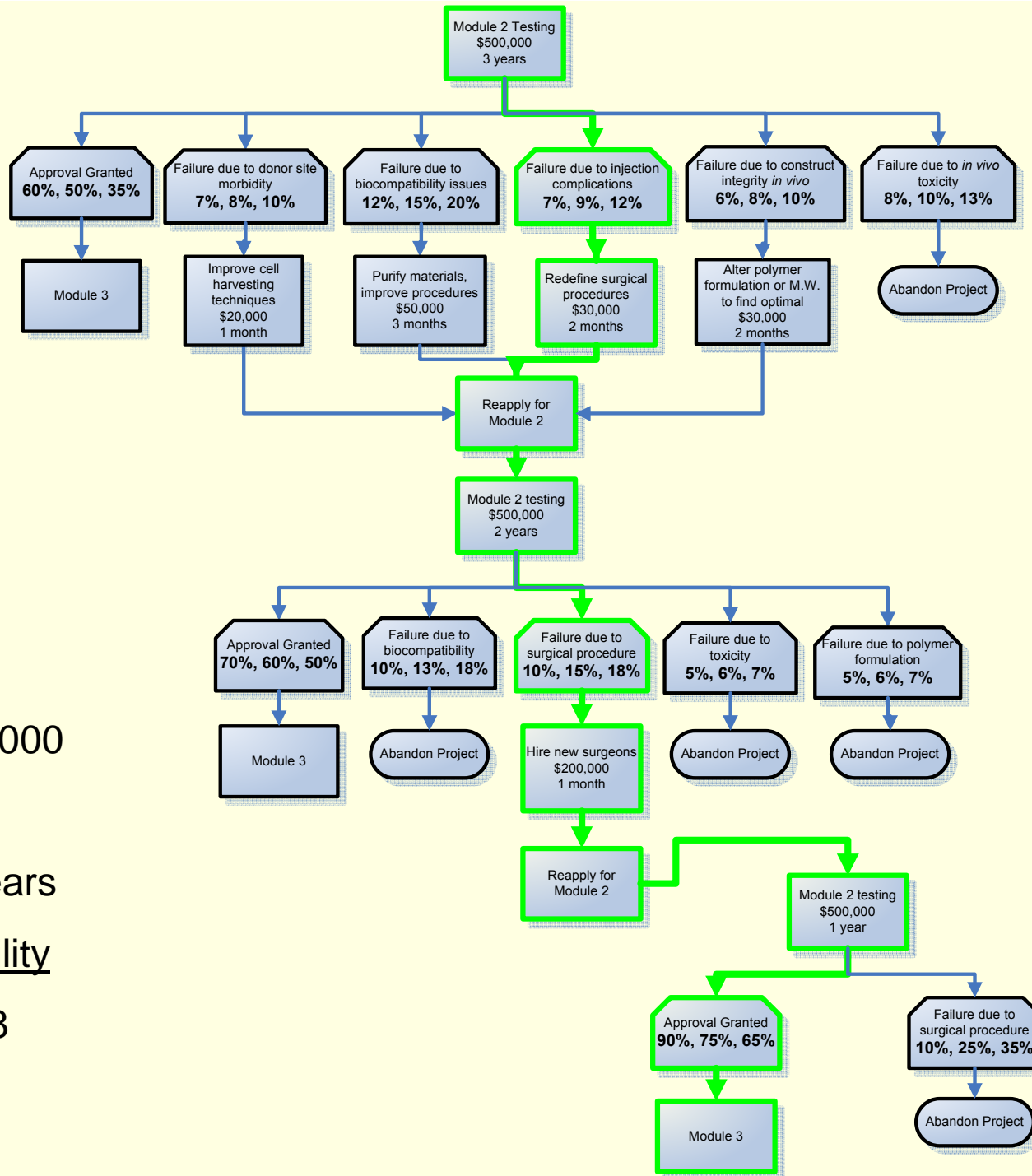
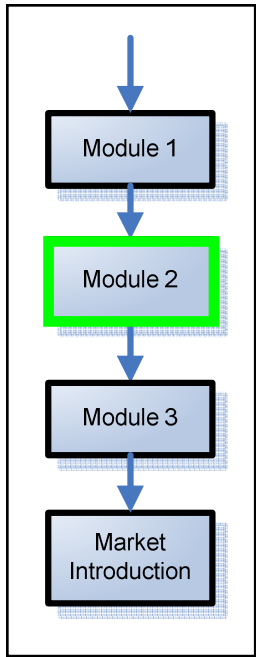
0.0015











Cost

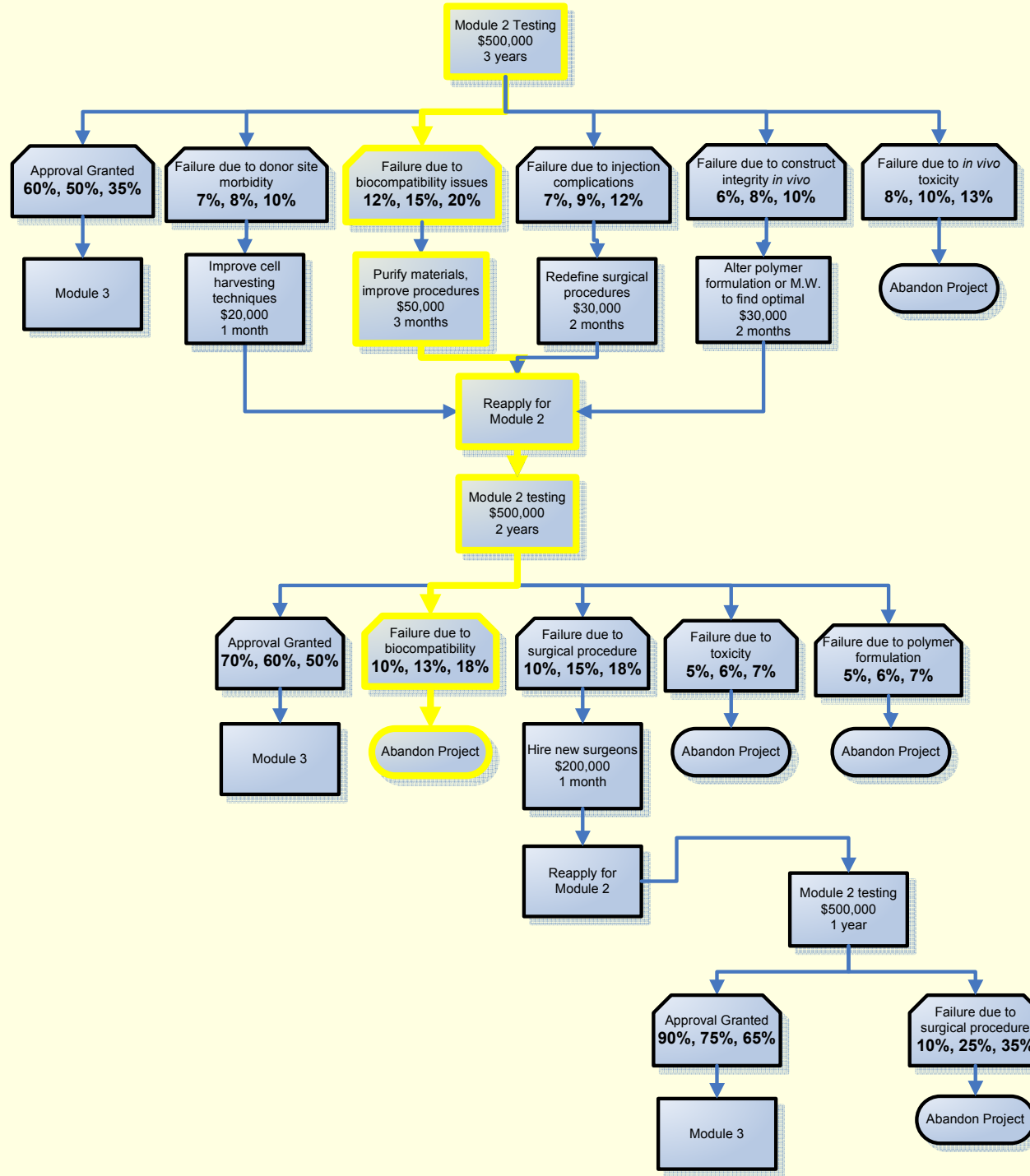
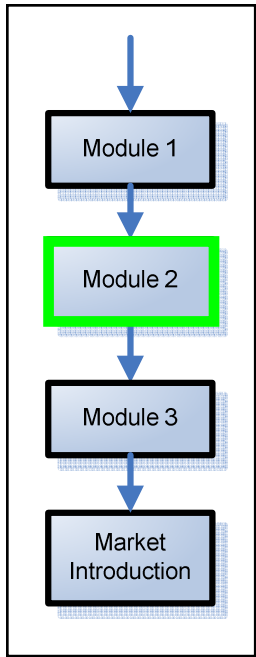
\$2,660,000

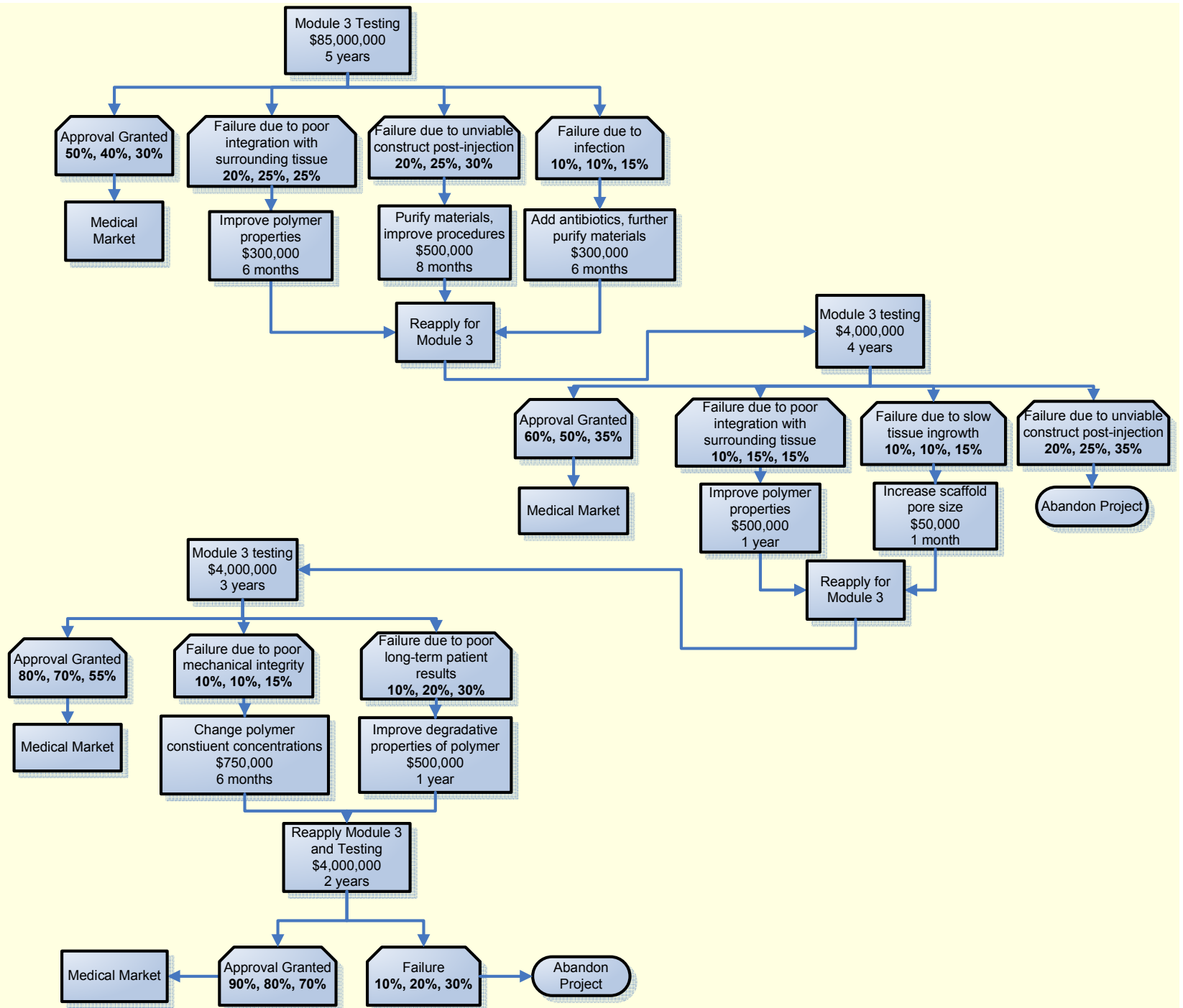
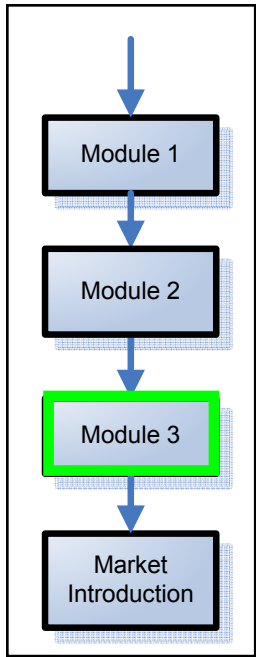
Time

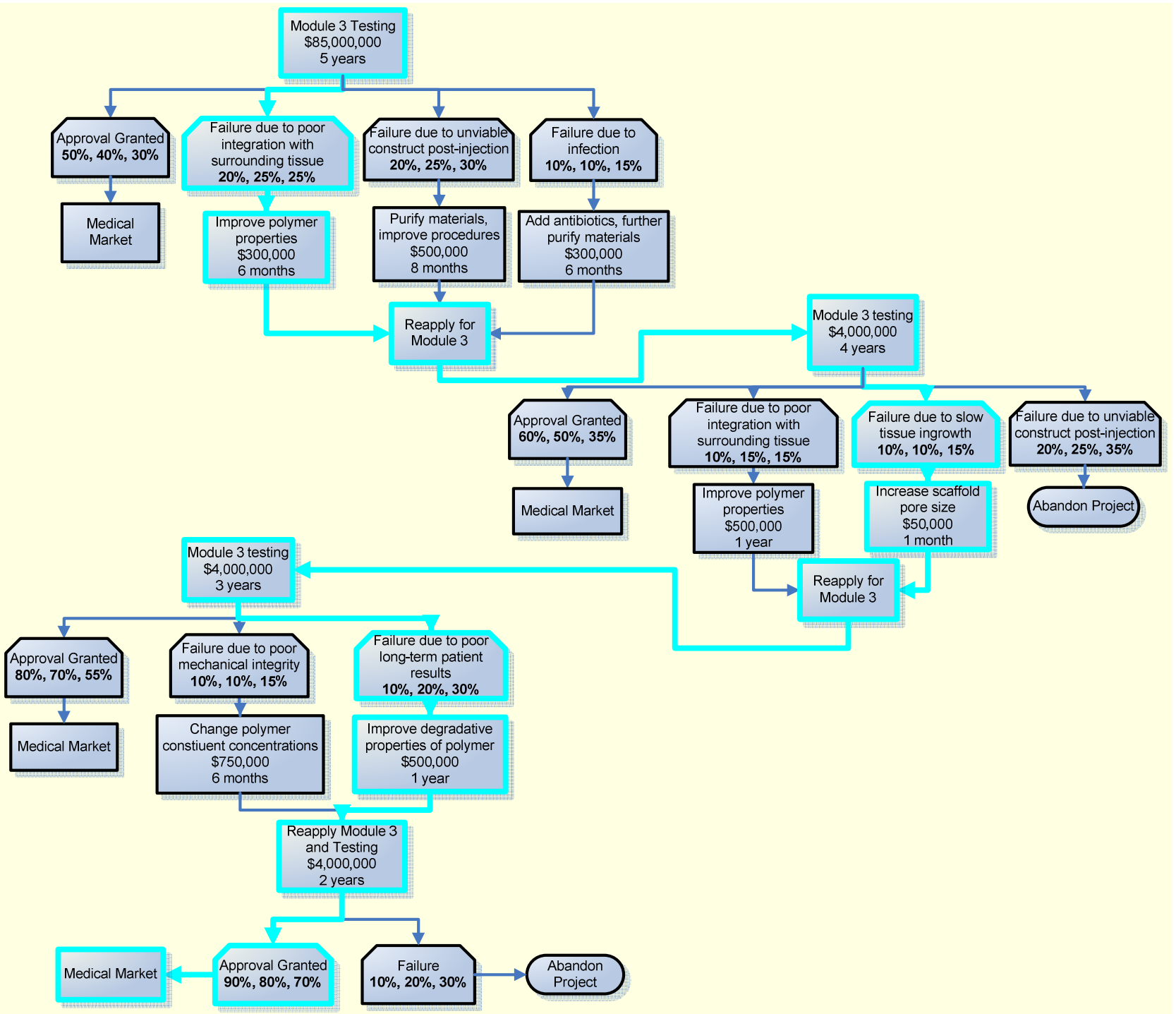
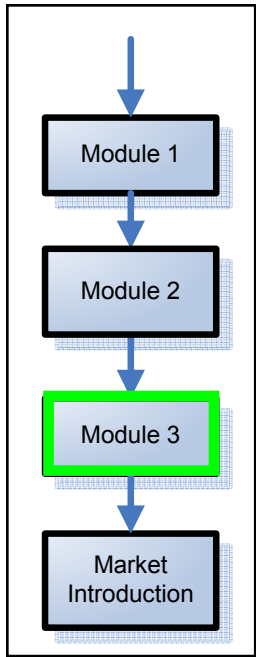
12.5 Years

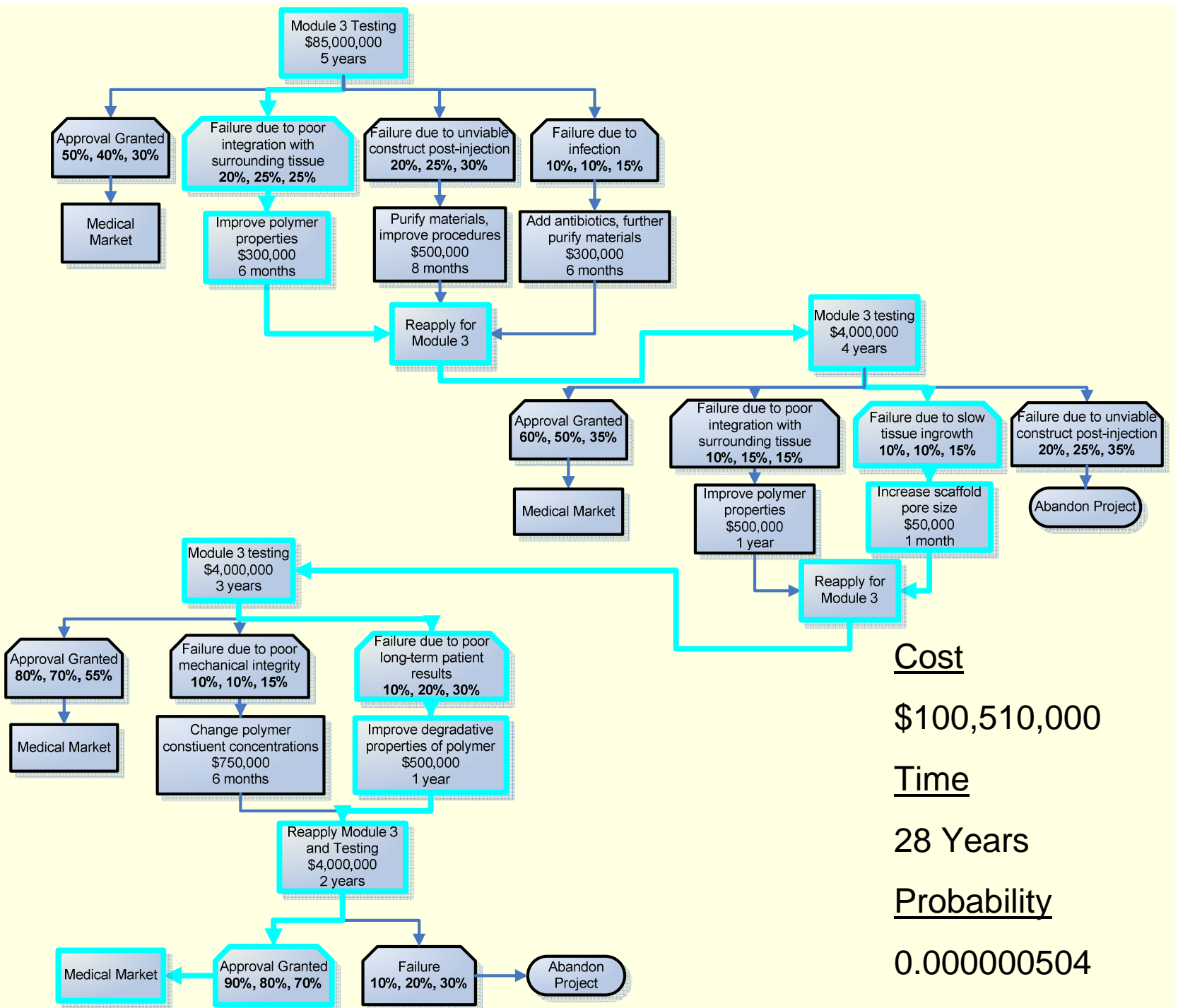
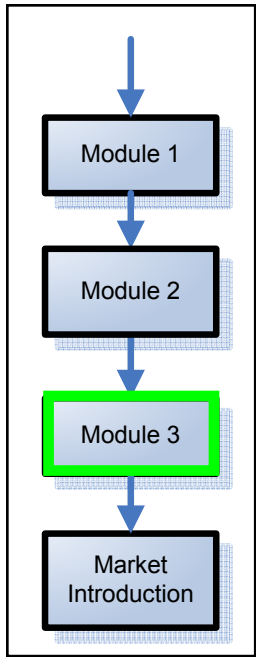
Probability

0.00028









Cost  
 \$100,510,000

Time  
 28 Years

Probability  
 0.000000504

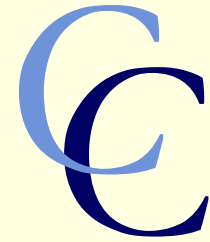
# Modeling Pathways



- Models can quickly become complicated
- 5,291 total pathways through FDA
  - 2,970 pathways lead to success
  - 2,321 pathways lead to failure
- First stage decisions shape FDA model
- Probabilities, time, and cost are estimated based on all available knowledge.
  - Modeling technical details increases accuracy of the FDA model.

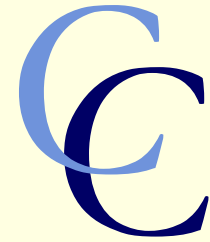


# Risk Assessment



- The probability, time until completion, and net present cost for each pathway was calculated
- Scenarios varying by the number of workers and the number of experiments were created
  - 2, 5, or 10 workers
  - 45, 60, or 70 experiments
- Net present worth of the product was calculated to evaluate the possible profit
  - Price and demand must be considered

# Pricing



- To know the expected value of each pathway, the profit for each operating year must be estimated.

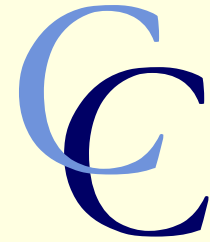
$$Profit_n = pd_n - IC_n d_n - FC_n$$

**IC** = Surgery and material cost per implant, **FC** = Fixed annual operating costs

- The price and demand are classically related by a simple expression

$$pd = Constant$$

# Pricing



- How do we choose a price?

## **Less than competitor:**

Get the majority of the market

Price: \$15,000

Demand: ~15,000

Profit: ~\$70,000,000

## **More than competitor:**

Get the smaller market share

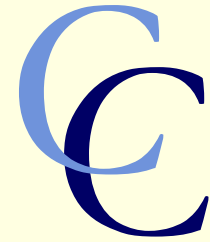
Price: \$35,000

Demand: ~7,000

Profit: ~\$170,000,000

- We will need a more detailed model to find the optimum price

# Pricing



- A more detailed pricing model involves maximizing consumer utility (happiness)
- With only one competitor, the utility (U) is:

$$U = d_1^\alpha + d_2^\beta$$

$\alpha = f$  (knowledge)

$\beta = f$  (happiness)

- This is maximized subject to two constraints:

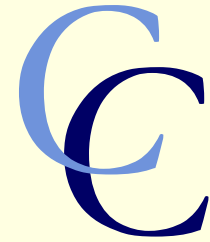
$$p_1 d_1 + p_2 d_2 \leq Y$$

$$d_1 + d_2 \leq D$$

Y = Total Consumer Budget

D = Total Demand

# Pricing



- This gives two possible equations relating demand and price:

Budget Controlled Solution

$$d_1 = \frac{\alpha}{\beta} \frac{p_2}{p_1} \left( \frac{Y - p_1 d_1}{p_2} \right)^{1-\beta} d_1^\alpha$$

Demand Controlled Solution

$$d_1 = \frac{\alpha}{\beta} (D - d_1)^{1-\beta} d_1^\alpha$$

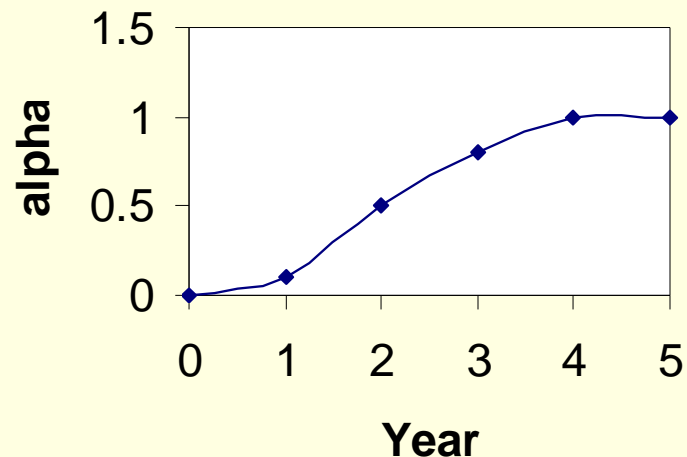
- These are both solved for  $d_1$ ; the lower solution satisfies both constraints.

# Pricing



## ■ Estimating $\alpha$ and $\beta$ :

Knowledge increases gradually until it becomes perfect ( $\alpha = 1$ )



$\beta$  is estimated by assuming happiness values and weights for various attributes

$$\beta = \frac{H_2}{H_1} = \frac{\sum w_i y_{2,i}}{\sum w_i y_{1,i}} = 0.8$$

Description	Weight	$y_1$	$y_2$
Long-term outcome	0.70	1	0.8
Invasiveness	0.15	0.8	0.4
Recovery Time	0.15	0.75	0.65

# Pricing



- Estimating Y and D
  - Values are assumed from knowledge of the competitor's current market and statistics on the number of people with this kind of knee problem.

$$Y = \$250,000,000 / \text{year}$$

$$D = 15,000 \text{ Implants} / \text{year}$$

# Pricing



- The demand and the profitability were evaluated for a range of prices.
- When  $\alpha = 1$ , the maximum profitability was found at:
  - $p_1 = \$95,000$
  - $d_1 = 2573$  Implants / year
  - Profit = \$217,000,000 / year
- This price was used to find profitability during the first five years

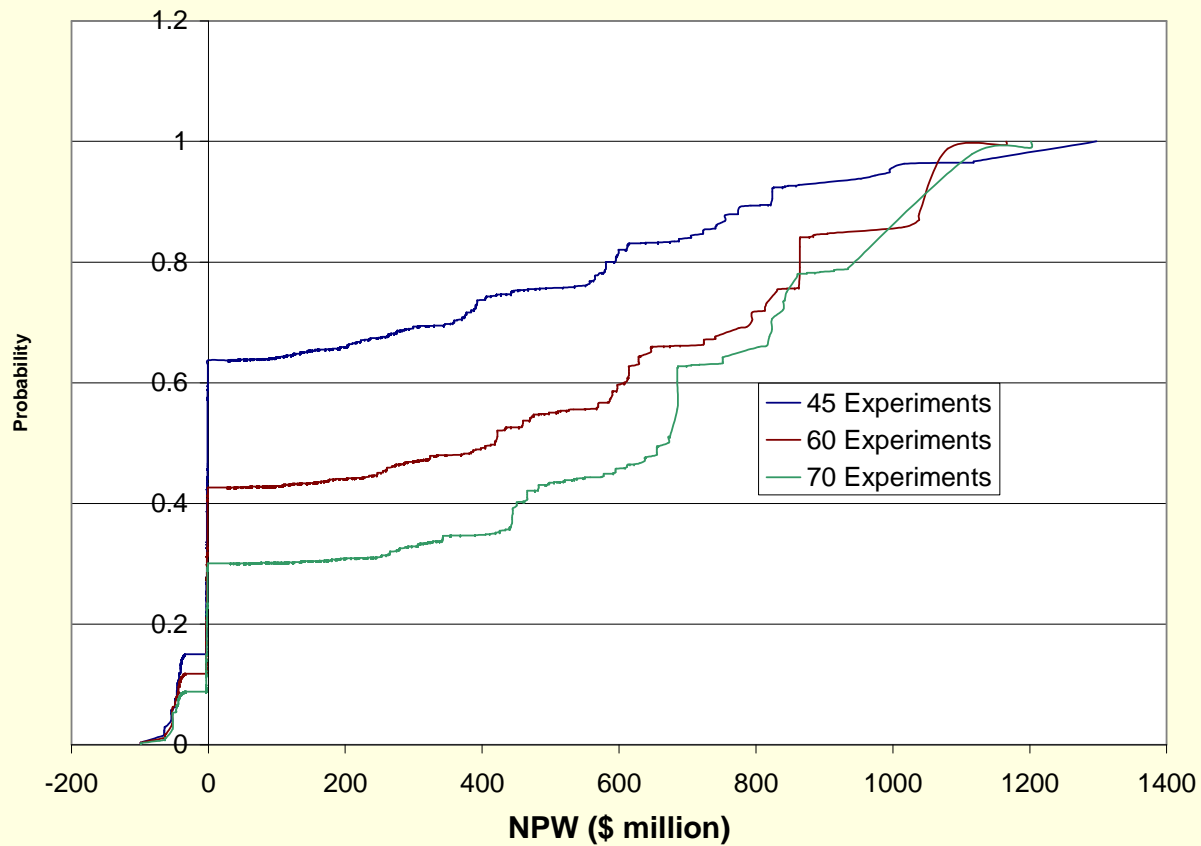
Year 1	Year 2	Year 3	Year 4	Year 5
\$0	-\$500,000	\$600,000	\$217,000,000	\$217,000,000



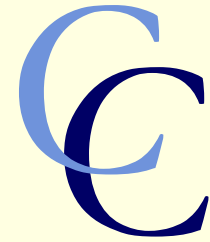
# Risk Curve



- These profits during operation give these risk curves for the NPW forty years from now



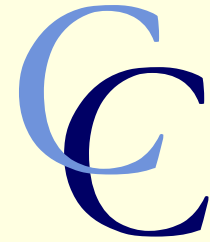
# Pricing Model Deviations



- The values used for  $\alpha$ ,  $\beta$ ,  $Y$ , and  $D$  are variable.
- To make this evaluation more rigorous, several values of each are used with their associated probabilities.

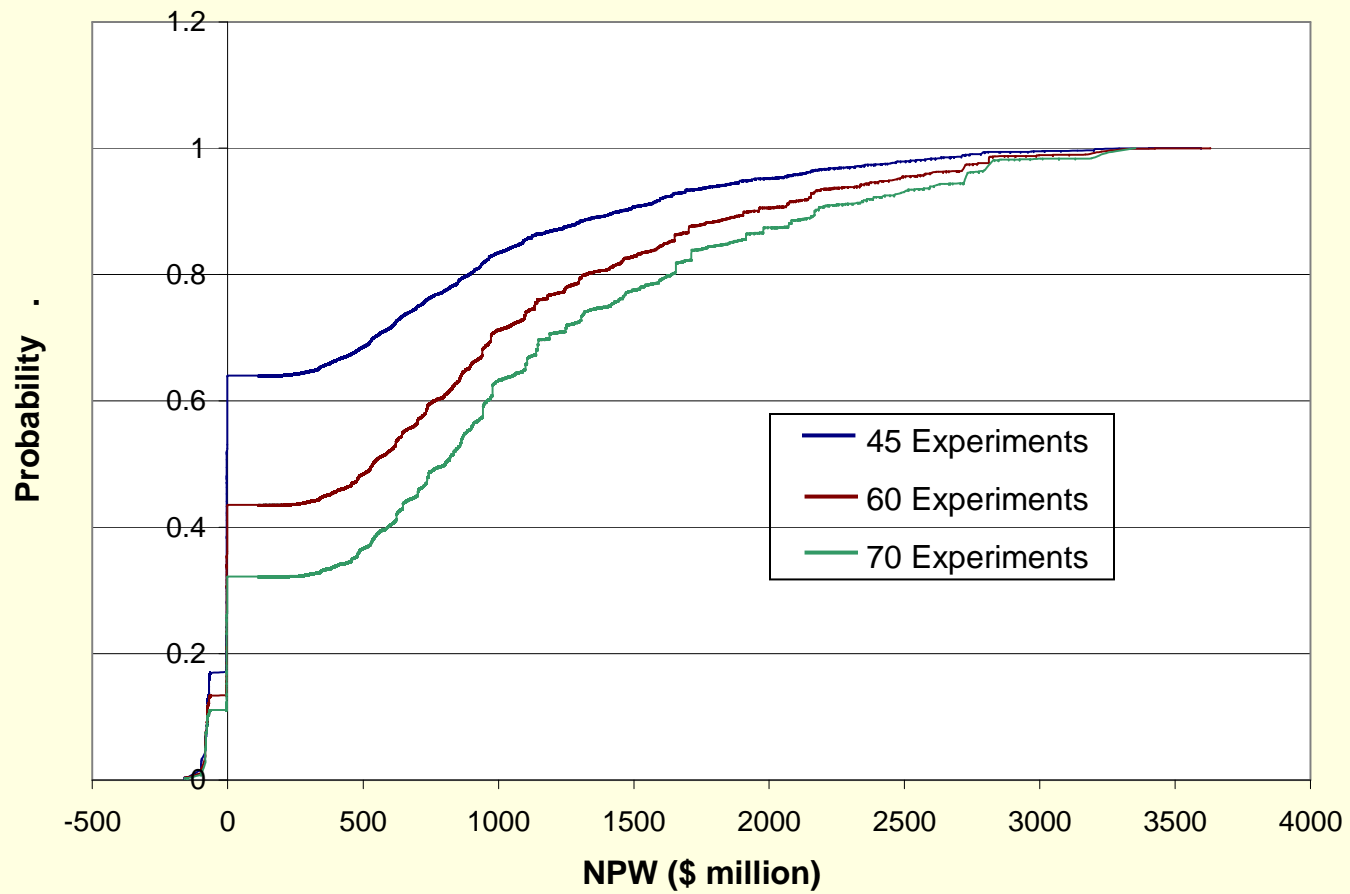
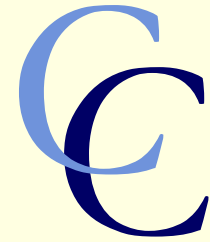
$\alpha$ (years to reach 1)	5 (50%)	4 (33%)	3 (17%)
$\beta$	0.5 (25%)	0.8 (50%)	0.999 (25%)
$Y$	\$150,000,000 (33%)	\$250,000,000 (33%)	\$400,000,000 (33%)
$D$	10,000 (33%)	15,000 (33%)	20,000 (33%)

# Profitability

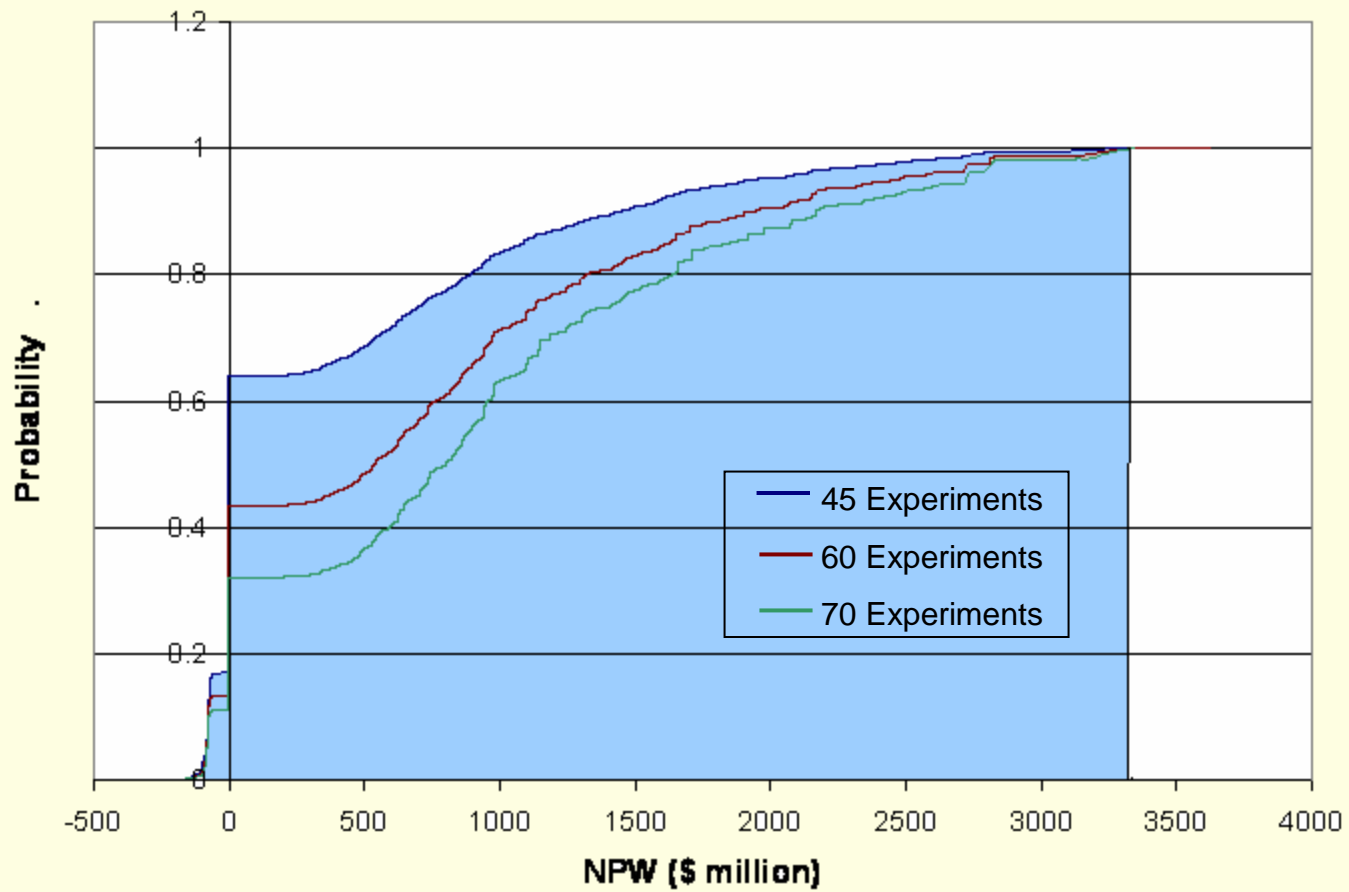


- The most profitable price for each scenario, is most strongly dependent on  $\beta$ .
- Changing D values have no effect on profitability; Budget constraint dominates at high prices.
- When products are almost equal ( $\beta = 1$ ), most profitable price is competitor's price.
- For low values of  $\beta$ , the most profitable price is surprisingly large - as much as \$590,000!
- We may want to charge lower prices to capture a larger segment of the market.

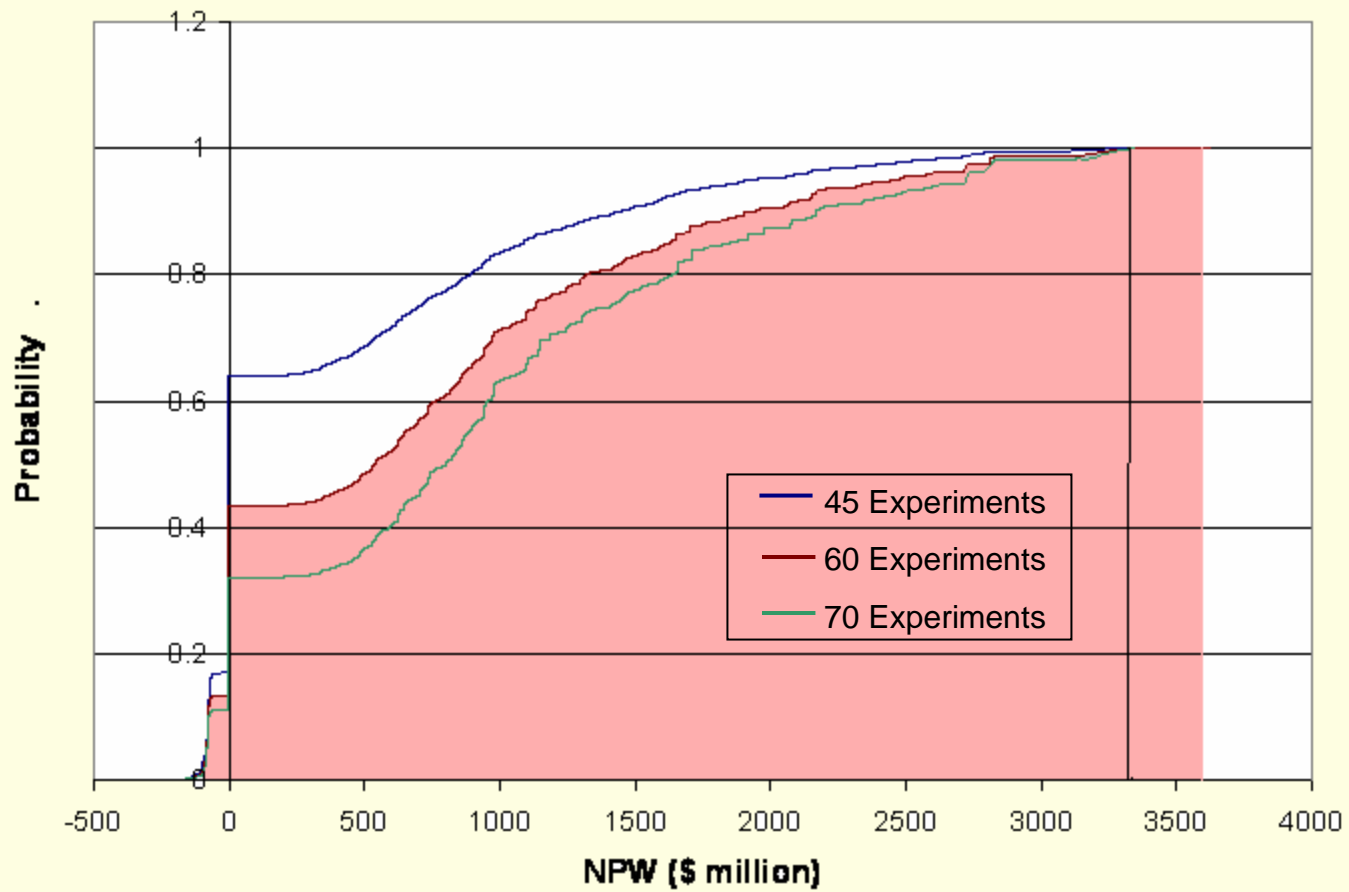
# 2 Workers



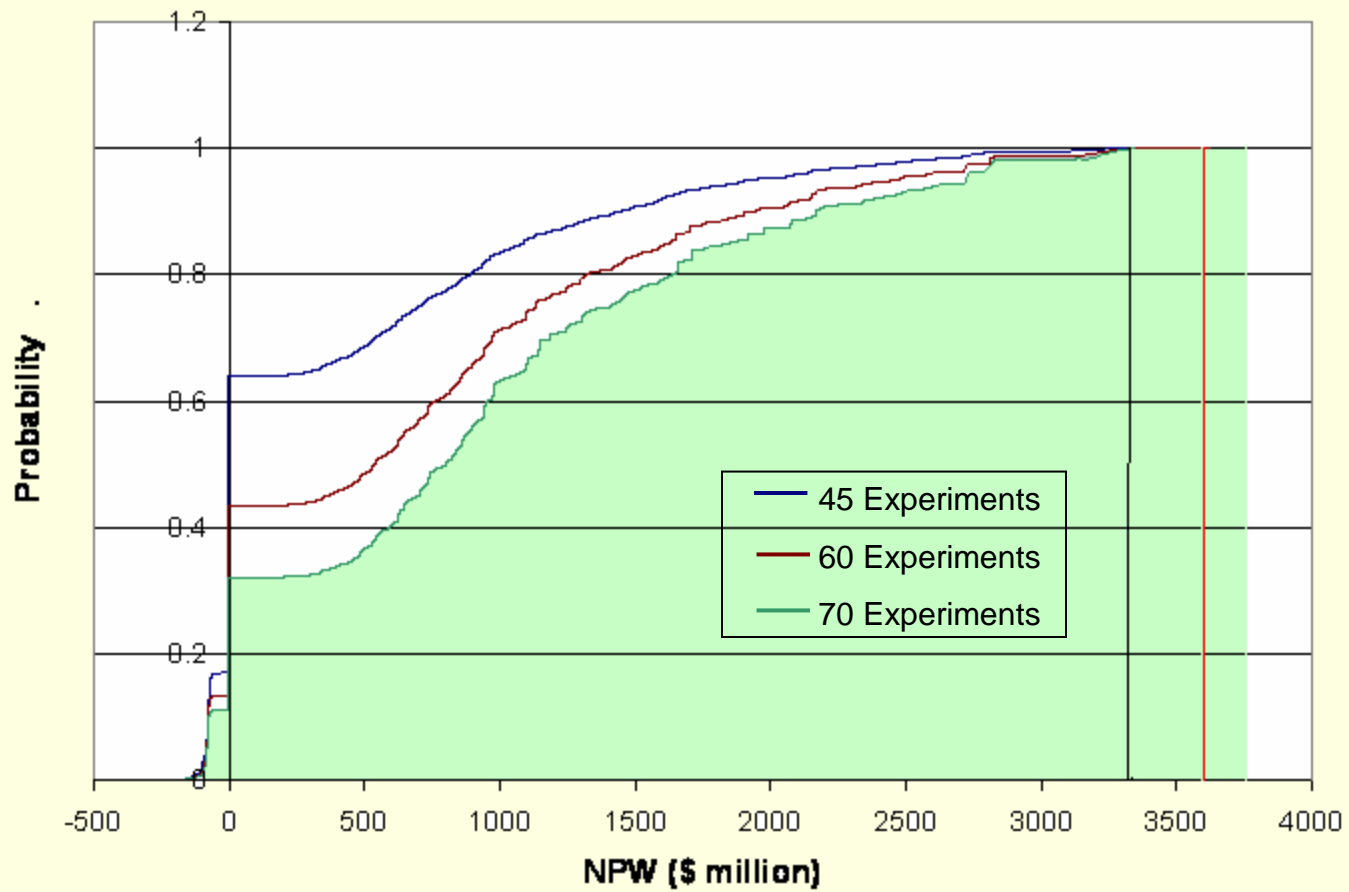
# 2 Workers



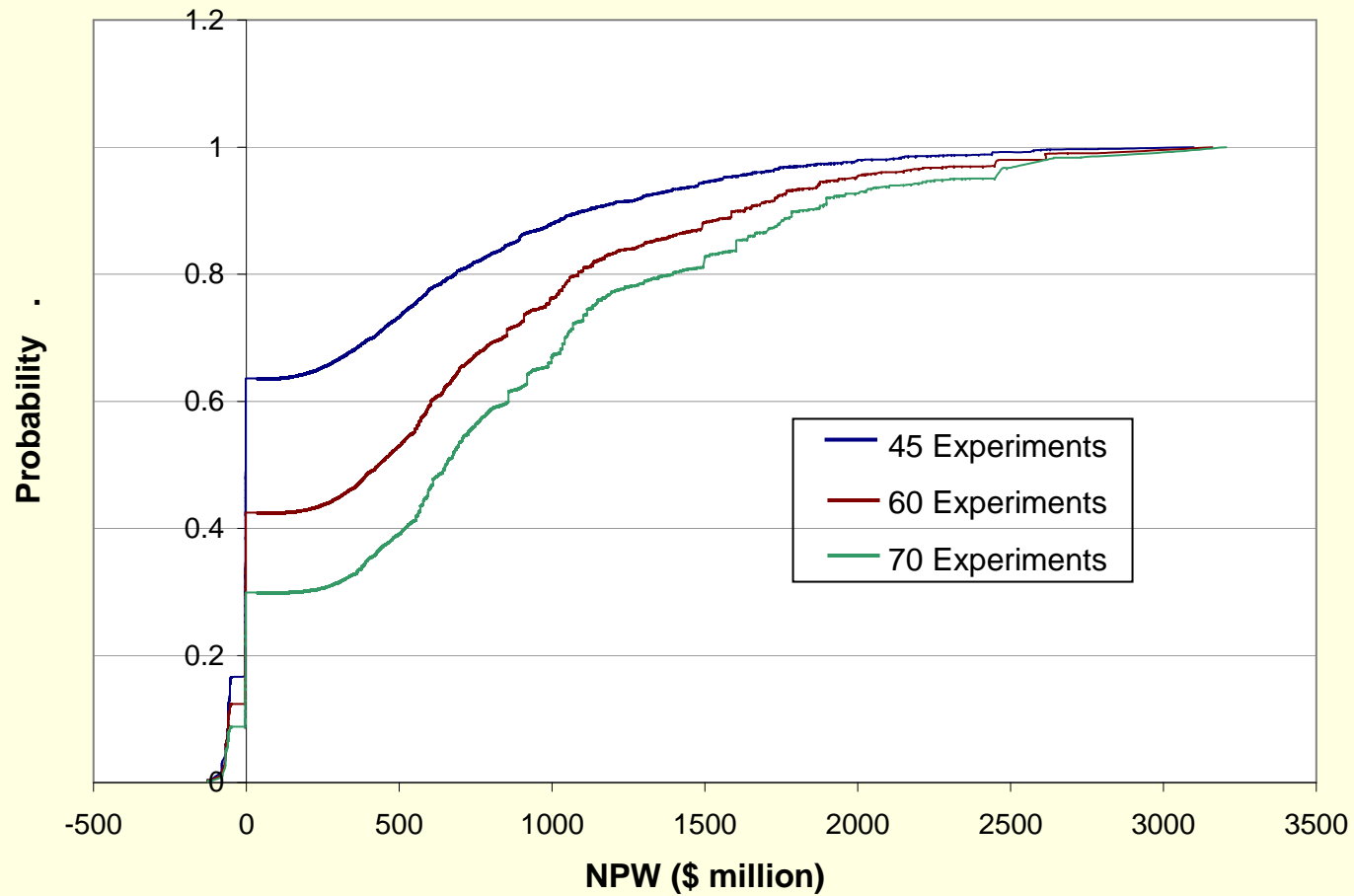
# 2 Workers



# 2 Workers

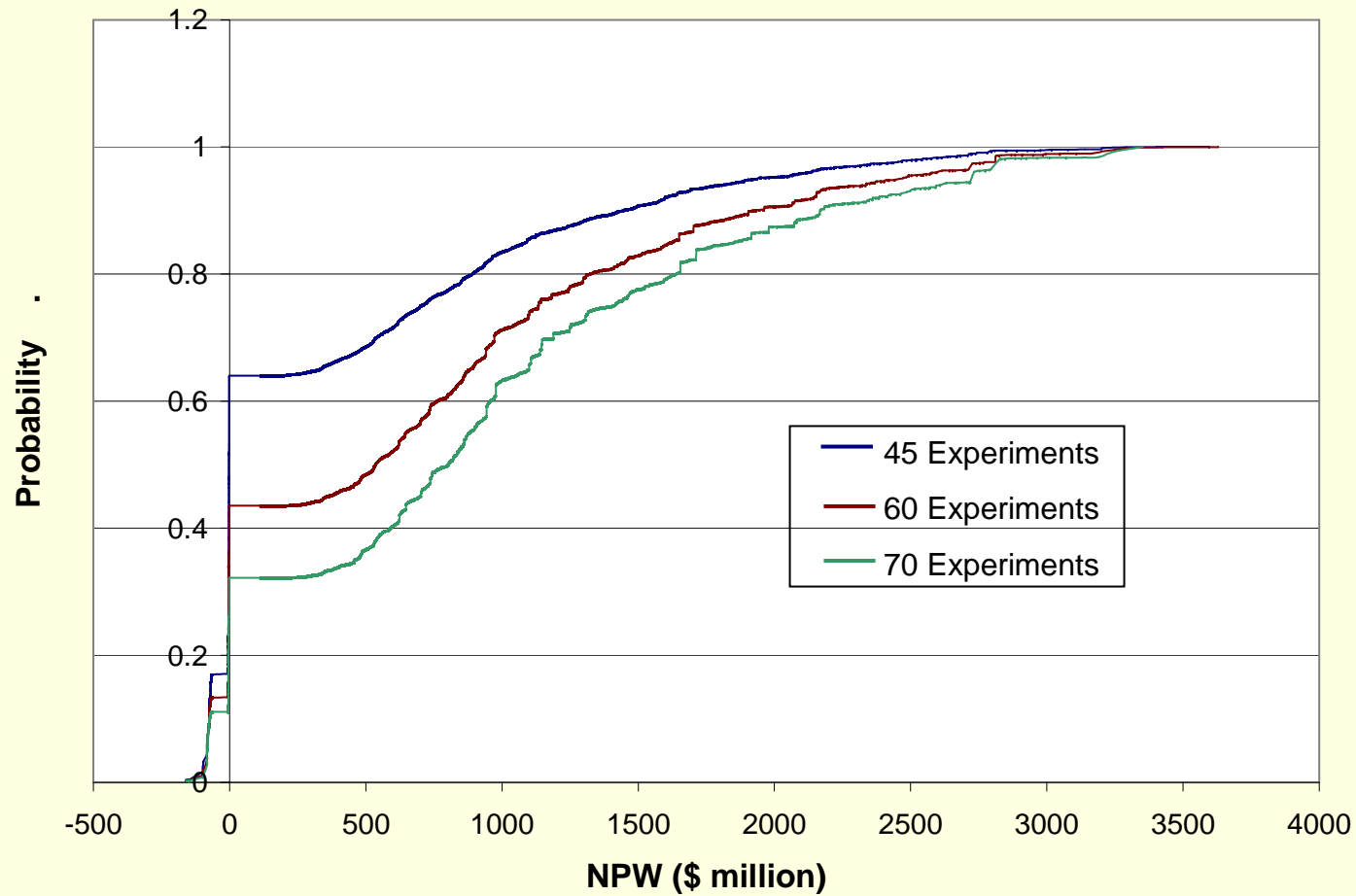
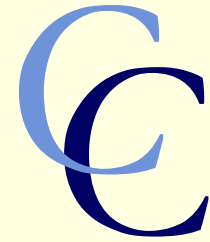


# 5 Workers

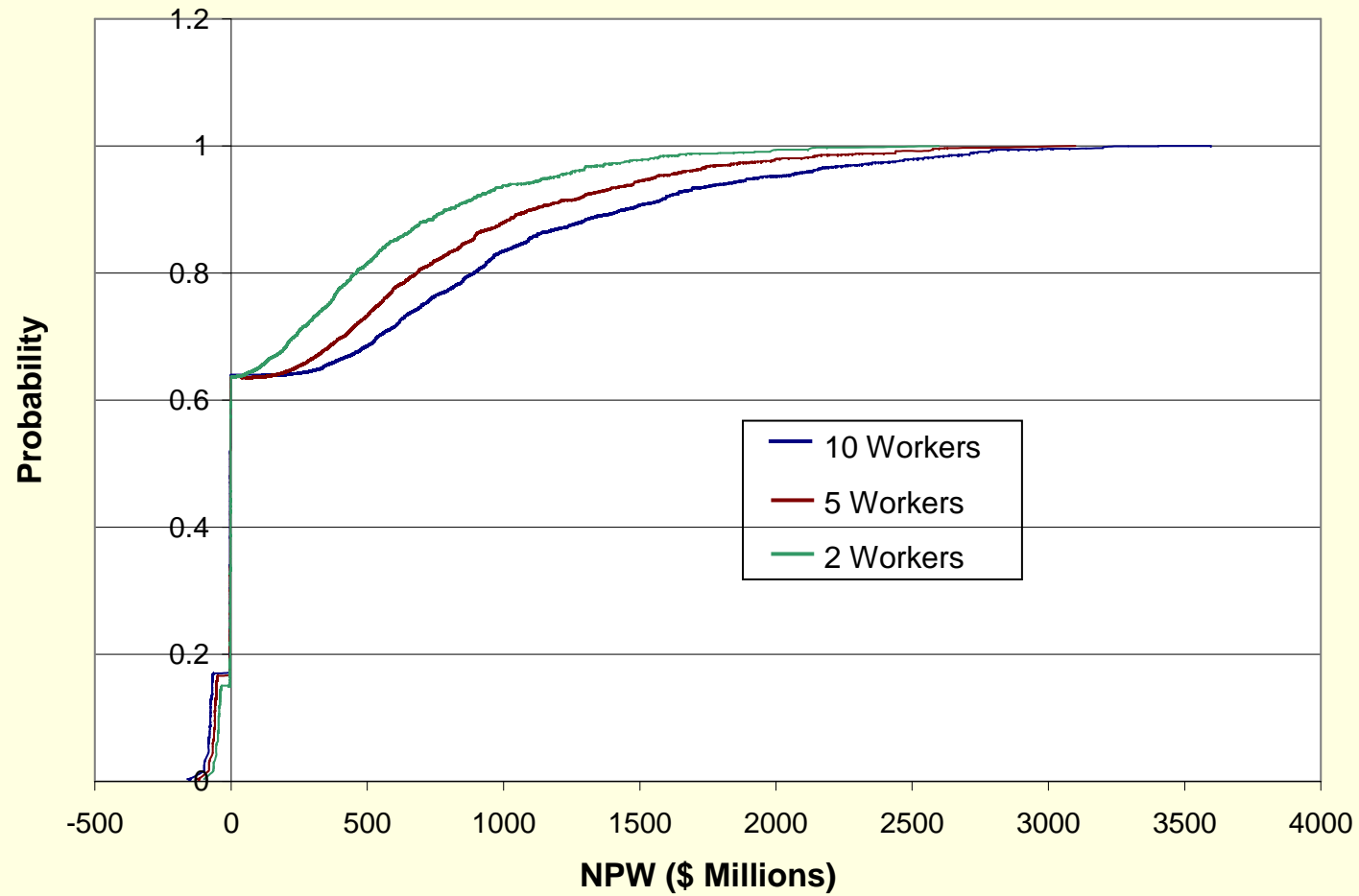




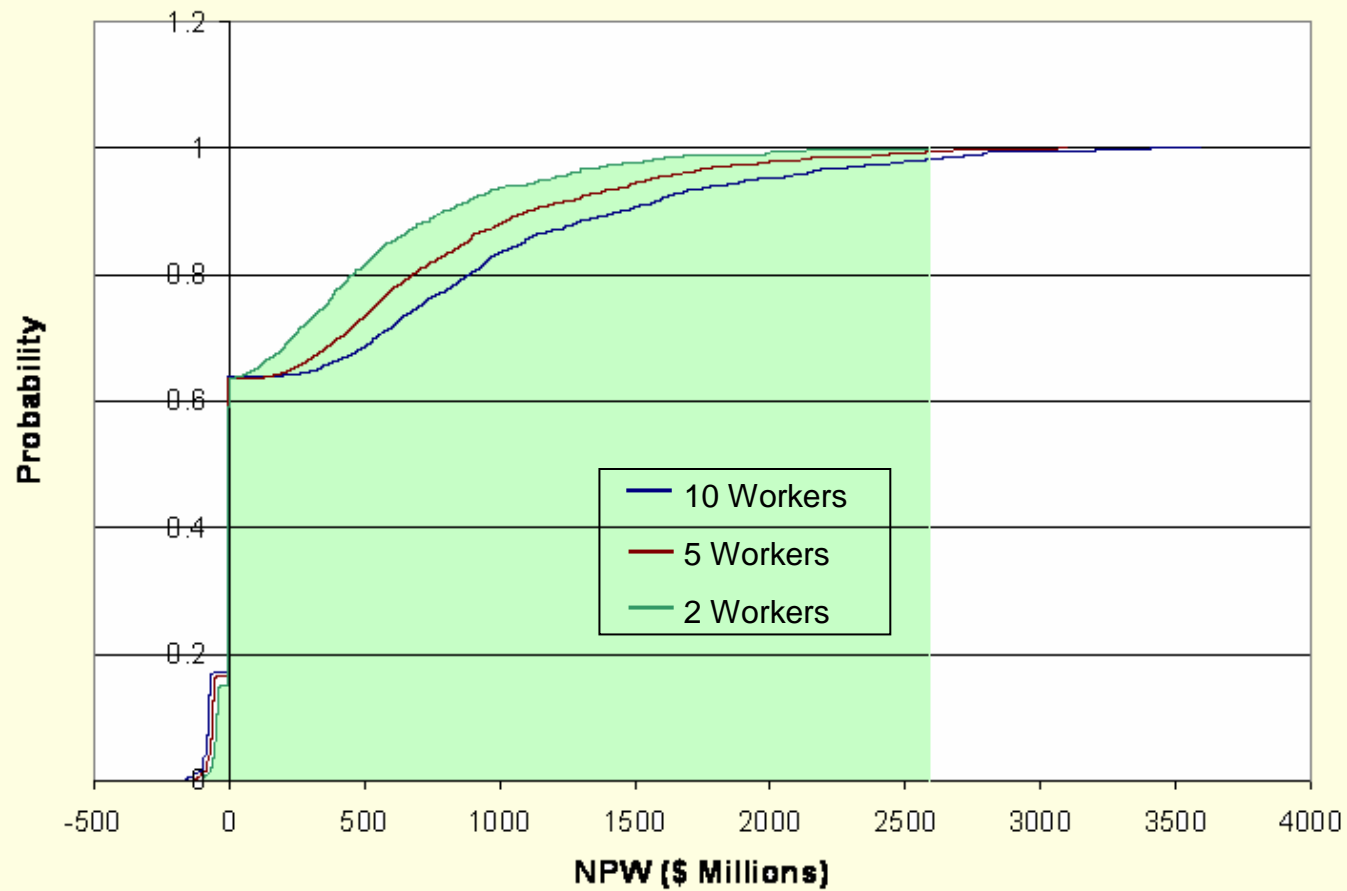
# 10 Workers



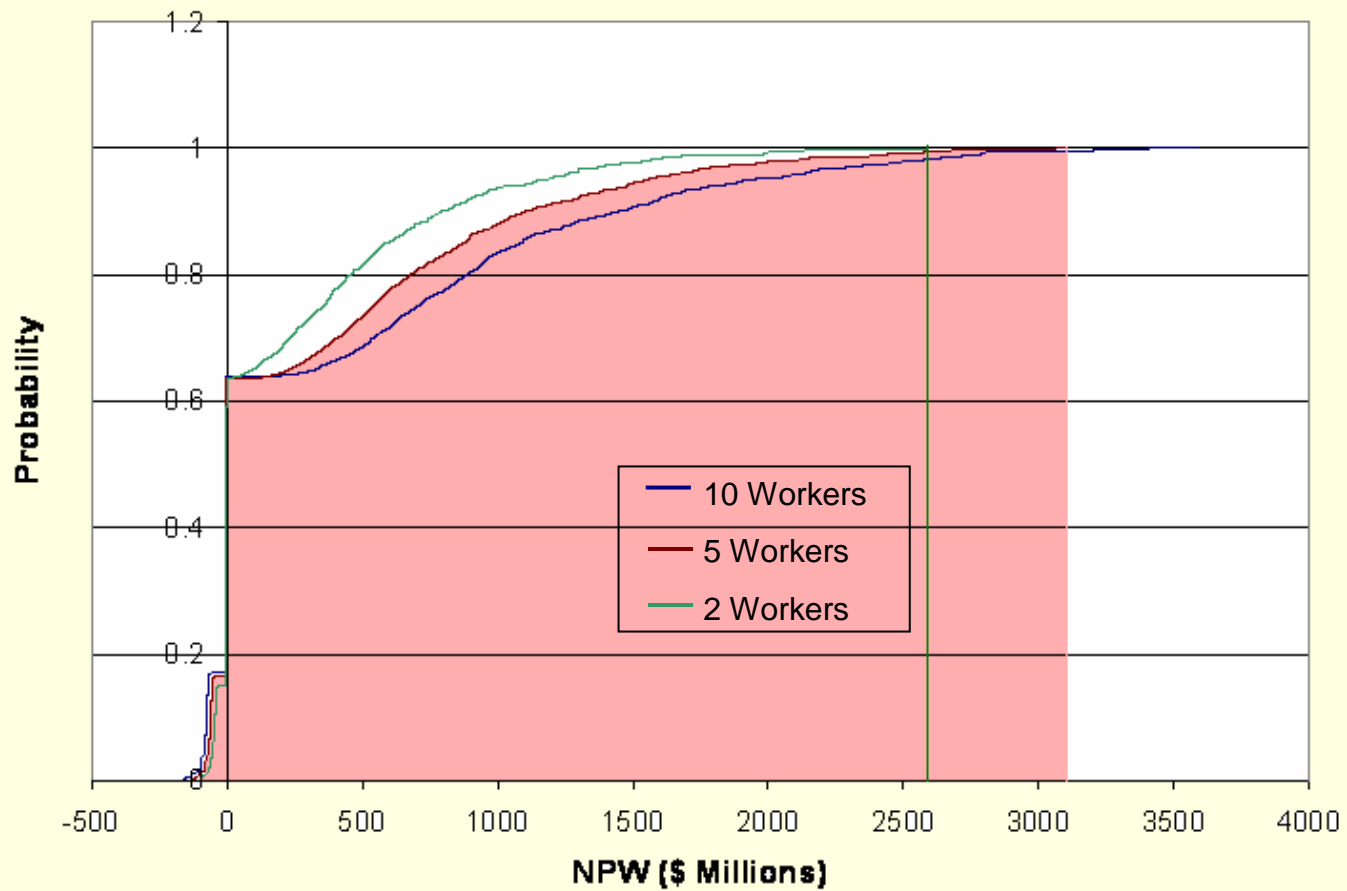
# 45 Experiments



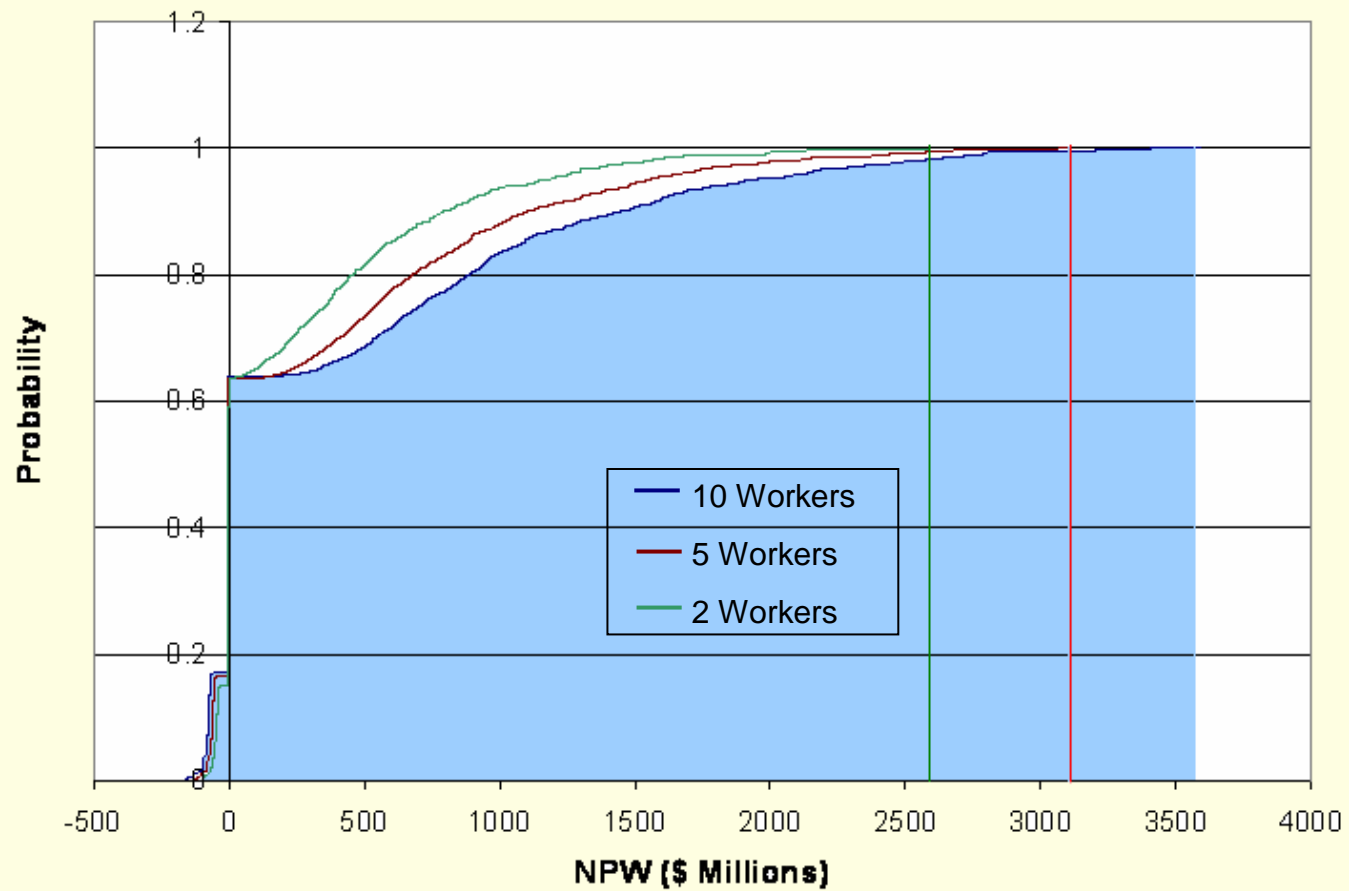
# 45 Experiments



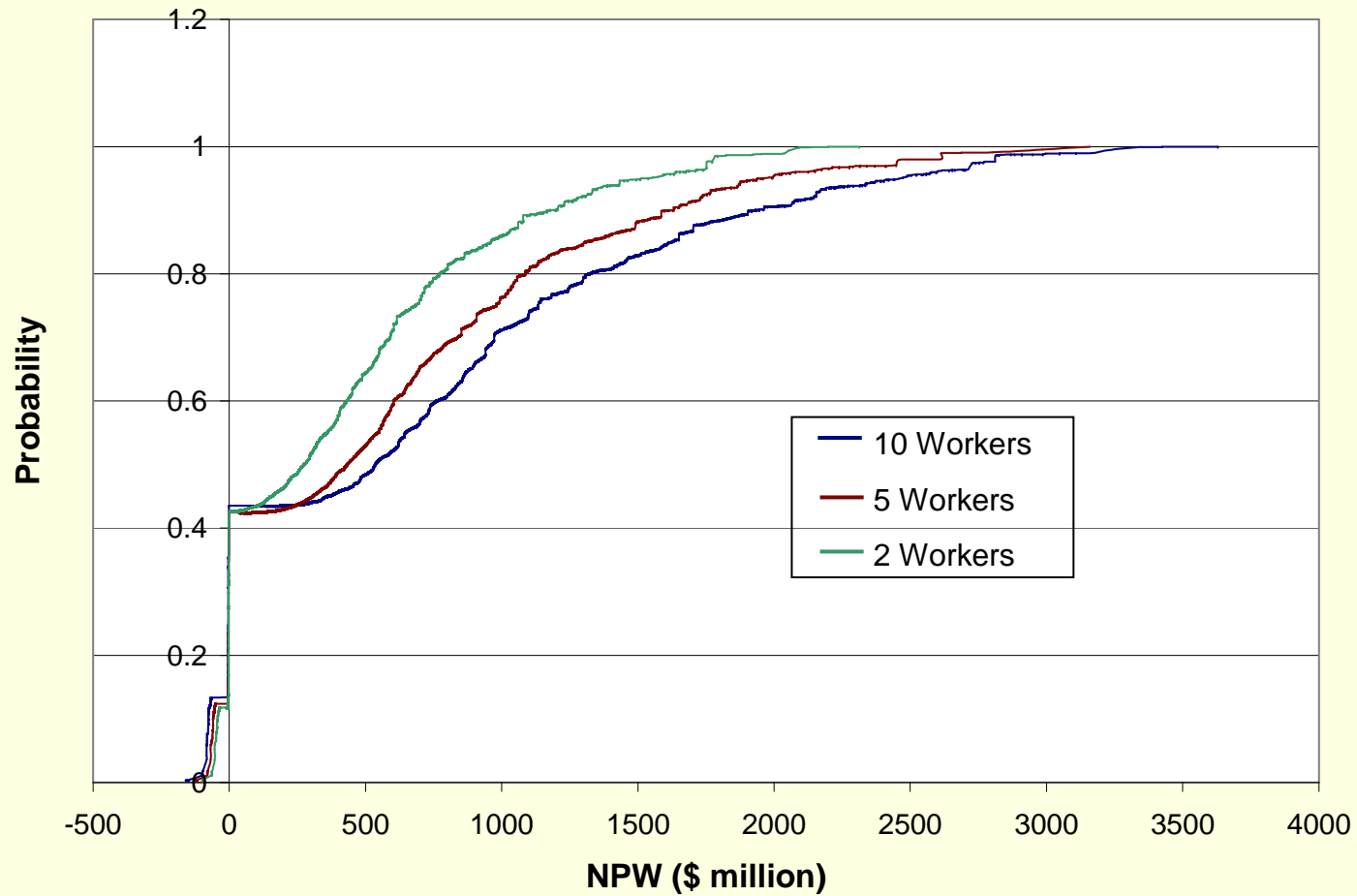
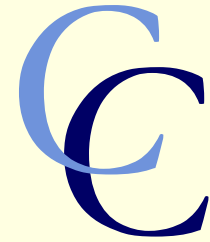
# 45 Experiments



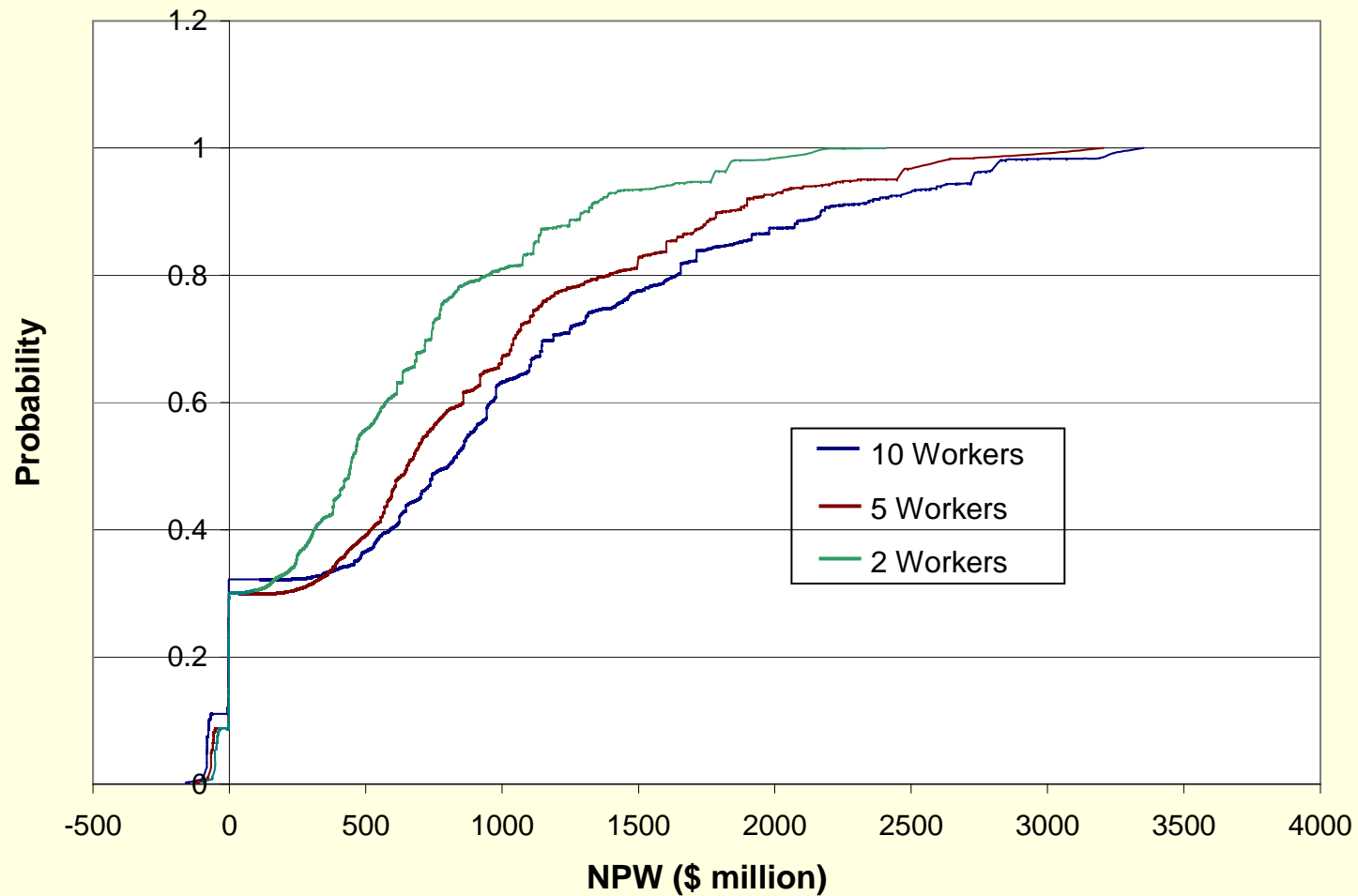
# 45 Experiments



# 60 Experiments



# 70 Experiments



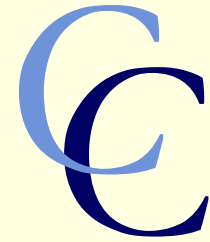
# Profitability Conclusions



- This process has the possibility of being remarkably profitable.
- The expected NPW can increase by:
  - Increasing the number of experiments
  - Increasing the number of workers
- The costs associated with these first stage decisions is minimal when compared to the possible gains.
- There are inherent limitations to how much the NPW would be expected to increase.



# Conclusions



- Cartilage damage is a problem that may be solved with a tissue engineered solution
- Mathematical modeling can help to guide experimentation and give insight into a process.
- The FDA process can be modeled, with first stage decisions taken into consideration.
- Risk analysis does have some limitations, but is useful in deciding if this procedure is a worthwhile investment.